

6  
5  
5  
6  
0

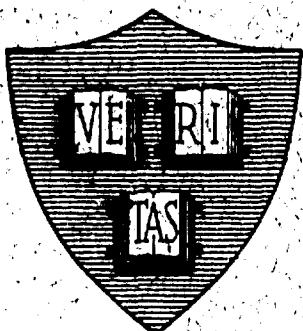
Office of Naval Research

Contract Nonr-1866(32)

NR-371-016

THE ADMITTANCE OF BARE CIRCULAR LOOP  
ANTENNAS IN A DISSIPATIVE MEDIUM

COPY



By

R.W.P King, C.W. Harrison, Jr.,  
D.G. Tingley

August 5, 1963

Technical Report No. 419

Crust Laboratory

Division of Engineering and Applied Physics  
Harvard University · Cambridge, Massachusetts

Published by  
NATIONAL TECHNICAL  
INFORMATION SERVICE  
U.S. Department of Commerce  
Washington, D.C. 20585

PRICES SUBJECT TO CHANGE

Office of Naval Research  
Contract Nonr-1866(32)  
NR - 371 - 016

THE ADMITTANCE OF BARE CIRCULAR LOOP  
ANTENNAS IN A DISSIPATIVE MEDIUM

by

R. W. P. King

C. W. Harrison, Jr.

D. G. Tingley

August 5, 1963

The research reported in this document was made possible through support extended Crust Laboratory, Harvard University, jointly by the Navy Department (Office of Naval Research), the Signal Corps of the U. S. Army, and the U. S. Air Force, under ONR Contract Nonr-1866 (32). Reproduction in whole or in part is permitted for any purpose of the United States Government.

Technical Report No. 419

Crust Laboratory  
Harvard University  
Cambridge, Massachusetts

#### ABSTRACT

The normalized input admittance of thin bare circular loop antennas has been evaluated from the theory of T. T. Wu. Computations have been made for loops in air and in an infinite homogeneous isotropic dissipative medium. A comparison is also made with Storer's theory of the loop. Numerical results are given in the form of graphs for several wire sizes and for loops up to 2.5 wavelengths in circumference. The properties of the medium are represented by the ratio  $\alpha/\beta$  in the range from zero (perfect dielectric) to one (good conductor);  $\alpha$  and  $\beta$  are the imaginary and real parts of the complex propagation constant  $k = \beta - j\alpha = \omega \sqrt{\mu} (\epsilon - j\sigma/\omega)$  where  $\mu$  is the permeability,  $\epsilon$  the dielectric constant and  $\sigma$  the conductivity of the medium.

## TABLE OF CONTENTS

	Page
<b>Introduction</b>	5
<b>Analytical Formulation</b>	5
<b>Evaluation of the Tables</b>	7
<b>Graphical Representation</b>	8
<b>Conclusion</b>	8
<b>List of References</b>	9

## LIST OF ILLUSTRATIONS

### Figure

1 Normalized conductance and susceptance of circular loop in air as a function of the number of terms - Wu's theory for $\beta b = 0.5$ and $2.0$ , $\Omega = 2 \ln(2\pi b/a) = 8 - 12$ . . . . .	10
2 Normalized susceptance of circular loop in a dissipative medium with propagation constant $k = \beta - ja$ as a function of the number of terms - Wu's theory for $\beta b = 2.0$ , $\Omega = 8, 12, 20$ , $a/\beta = 0 - 1$ . . . . .	11
3 Normalized admittance of circular loop antenna in a dissipative medium - Wu's theory, $\Omega = 10$ . . . . .	12
4 Normalized admittance of circular loop antenna in a dissipative medium - Wu's theory, $\Omega = 11$ . . . . .	13
5 Normalized admittance of circular loop antenna in a dissipative medium - Wu's theory, $\Omega = 12$ . . . . .	14
6 Normalized admittance of circular loop antenna in a dissipative medium - Wu's theory, $\Omega = 15$ . . . . .	15
7 Normalized admittance of circular loop antenna in a dissipative medium - Wu's theory, $\Omega = 17.5$ . . . . .	16
8 Normalized admittance of circular loop antenna in a dissipative medium - Wu's theory, $\Omega = 20$ . . . . .	17

## LIST OF TABLES

TABLE I	Normalized Admittance $Y/\Delta$ of Loop Antennas in Dissipative Media . . . . .	18-19
TABLE II	Normalized Admittance $Y/\Delta$ of Loop Antennas in Dissipative Media . . . . .	20-21
TABLE III	Normalized Admittance $Y/\Delta$ of Loop Antennas in Dissipative Media . . . . .	22-23
TABLE IV	Normalized Admittance $Y/\Delta$ of Loop Antennas in Dissipative Media . . . . .	24-25
TABLE V	Normalized Admittance $Y/\Delta$ of Loop Antennas in Dissipative Media . . . . .	26-27
TABLE VI	Normalized Admittance $Y/\Delta$ of Loop Antennas in Dissipative Media . . . . .	28-29

## THE ADMITTANCE OF BARE CIRCULAR LOOP ANTENNAS IN A DISSIPATIVE MEDIUM

### Introduction

The first general analysis of the circular loop as a transmitting antenna appears to be that of Hallen<sup>1</sup>; he used the method of expansion in Fourier series. However, owing to the occurrence of a singularity or a very large value when the number of terms in the summation is sufficiently great, Hallen concluded that the series was divergent. Storer<sup>2</sup> avoided the contribution from the large term by replacing the Fourier series by the corresponding integral and evaluating this in the sense of the Cauchy principal value. He provided extensive tables and graphs of the impedance, admittance, and distribution of current for loops up to a wavelength in circumference with a number of different wire sizes. Recently, Wu<sup>3</sup> re-examined the problem of evaluating the Fourier series. He considered Storer's expedient to be of doubtful validity and devised an alternative and improved method with approximations that are valid over larger ranges of the parameters.

Although formulated specifically for loops in air, the solutions of both Wu and Storer are readily applied to loops in an infinite homogeneous and isotropic medium by the introduction of the constitutive parameters of the medium at the appropriate points. It is the purpose of this paper to discuss the evaluation of the admittance of a loop antenna in an arbitrary dissipative medium from Wu's formula. A comparison with Storer's results is also provided.

Since loops up to a wave length in circumference are considered, the present work is a significant extension of the earlier studies by Kraichman<sup>4</sup> and by Chen and King.<sup>5</sup> Kraichman's analysis is based on a postulated uniform distribution of current around the loop which is valid only for electrically extremely small loops if these are bare or covered with a very thin layer of dielectric. The work of Chen and King makes use of Storer's analysis but retains only the first two terms in the Fourier Series. Although this is a considerably better approximation than that of Kraichman, it is also limited to electrically rather small loops. Indeed, even for loops with circumferences as small as  $0.1\lambda$  to  $0.3\lambda$ , a surprisingly large error in the normalized conductance is made when only the first two terms in the Fourier series are retained.

### Analytical Formulation

The admittance of a circular loop of radius  $b$  when made of wire of radius  $a$  has been derived by Storer<sup>2</sup> and, in a somewhat more general form, by Wu<sup>3</sup> specifically for antennas in air. The generalized formula for the normalized admittance  $Y/\Delta = G/\Delta + jB/\Delta$  of a loop in an infinite homogeneous and isotropic dissipative medium when driven by a delta-function generator is

$$\frac{Y}{\Delta} = \frac{-j(1 - j\alpha/\beta)}{\pi \zeta_0} \left[ \frac{1}{\epsilon_0} + 2 \sum_{n=1}^{\infty} \frac{1}{a_n} \right] \quad (1)$$
$$\zeta_0 = (\mu_0 / \epsilon_0)^{1/2} \approx 120 \text{ mohms}$$

where

$$a_n = \frac{kb}{2} (K_{n+1} + K_{n-1}) - \frac{n^2}{kb} K_n. \quad (2)$$

In this formula

$$K_o = \frac{1}{\pi} \ln \frac{8b}{a} - \frac{1}{2} \left[ \int_0^{2kb} \Omega_o(x) dx + j \int_0^{2kb} J_o(x) dx \right] \quad (3)$$

$$K_n = K_{-n} = \frac{1}{\pi} \left[ J_o\left(\frac{na}{b}\right) J_o\left(\frac{na}{b}\right) + C_n \right] - \frac{1}{2} \left[ \int_0^{2kb} \Omega_{2n}(x) dx + j \int_0^{2kb} J_{2n}(x) dx \right] \quad (4)$$

$$C_n = \ln(4n) + 0.5772\dots - 2 \sum_{m=0}^{n-1} (2m+1)^{-1} \quad (5)$$

where  $J_o(z)$  and  $J'_o(z)$  are the modified Bessel functions of the first and second kinds and  $\Omega(x)$  is the Lommel-Weber function defined by

$$\Omega_m(x) = \frac{1}{\pi} \int_0^\pi \sin(x \sin \theta - m\theta) d\theta. \quad (6)$$

In (2)

$$k = \beta - j\alpha = \omega \sqrt{\mu(\epsilon - j\sigma/\omega)} = \omega \sqrt{\mu\epsilon} [f(p) - jg(p)] \quad (7)$$

is the complex propagation constant. In (7)

$$p = \sigma/\omega\epsilon \quad (8)$$

is the loss tangent of the medium and the  $f(p)$  and  $g(p)$  functions are defined as follows:

$$f(p) \pm jg(p) = \sqrt{1 \pm jp}. \quad (9)$$

This is equivalent to

$$f(p) = \cosh\left(\frac{1}{2} \sinh^{-1} p\right), \quad g(p) = \sinh\left(\frac{1}{2} \sinh^{-1} p\right). \quad (10)$$

The functions  $f(p)$  and  $g(p)$  are extensively tabulated in the literature.<sup>6,7</sup>

In order to provide generally useful graphs and tables of the admittance of a loop antenna when immersed in a medium characterized by arbitrary values of  $\sigma$  and  $\epsilon$ , it is convenient to introduce the normalizing factor

$$\Delta = \sqrt{\frac{\epsilon_r}{\mu_r}} f(p) \quad (11)$$

where  $\epsilon_r$  and  $\mu_r$  are the relative dielectric constant and permeability. This factor appears in (1), for antennas in air, it is equal to unity.

As with a dipole antenna when center driven by a delta-function generator, the admittance  $Y$  strictly does not exist, since its susceptance must become infinite owing to the knife-edge terminals with zero separation that characterize the delta-function generator. However, as shown for the dipole,<sup>8,9</sup> the representation of the current by continuous functions combined with the extreme localization of that part of the current that is associated with the knife edges of the generator, effectively omits the latter for thin wires unless a very large number of terms in the Fourier series is taken. If the infinite sum in (1) is replaced by a sum over a finite number of terms, an approximate formula is obtained that is a good measure of the admittance of the antenna for use with a practical method of driving when combined with a suitable terminal-zone network.

#### Evaluation of the Tables

The formula (1) was evaluated on a high-speed computer using successively 8, 9, 10, 18, 19, and 20 terms in the series. The normalized conductance  $G/\Delta$  and normalized susceptance  $B/\Delta$  for  $\alpha/\beta = 0$  are shown in Fig. 1 as a function of the number of terms in the series. Curves are shown for  $\beta b = 0.5$  and 2.0 and for  $\Omega = 2 \ln(2\pi b/a) = 8, 9, 10, 11$ , and 12. It is seen that the convergence is such that  $G/\Delta$  does not change noticeably for both values of  $\beta b$  and for all values of  $\Omega$ . On the other hand,  $B/\Delta$  continues to increase with the number of terms. The rate of this increase is great when  $\Omega < 10$  and when  $\beta b$  is large; it is quite small for  $\Omega \geq 10$ , especially when  $\beta b$  is small. In general, it may be concluded that when  $\Omega \geq 10$ , 20 terms in the Fourier series yield highly accurate values of  $G/\Delta$  for  $\beta b \leq 2.5$ , quite good values of  $B/\Delta$  for  $\beta b < 1$ , and fair values when  $1 \leq \beta b \leq 2.5$ .

The values of  $G/\Delta$  and  $B/\Delta$  evaluated from Storer's theory<sup>2</sup> are indicated on the right in Fig. 1. It is seen that they are in excellent agreement with Wu's results using 20 terms insofar as  $G/\Delta$  is concerned, but that significant differences occur in  $B/\Delta$ .

In Fig. 2 values of  $B/\Delta$  are shown as functions of the number of terms in the Fourier series for  $\beta b = 2.0$  with  $\Omega = 8, 12$ , and 20, when  $\alpha/\beta$  is increased from zero to one. It is seen that except for  $\alpha/\beta = 1$ , the curves for the relatively thick-wire loop with  $\Omega = 8$  or  $2\pi b/a = 27.3$  increase significantly with the number of terms. On the other hand, the curves for the thinner loops with  $\Omega = 12$  ( $2\pi b/a = 259$ ) and  $\Omega = 20$  ( $2\pi b/a = 11,013$ ) are practically independent of the number of terms for all values of  $\alpha/\beta$ .

These results indicate that a Fourier series solution in which 20 terms are retained is satisfactory for determining the admittance of thin-wire loops ( $\Omega \geq 10$ ) that are not too large ( $\beta b \leq 2.5$ ) when in air or an arbitrary dissipative medium. The approximation is excellent for the conductance, somewhat less accurate for the susceptance. Numerical values of the normalized admittance  $Y/\Delta = G/\Delta + jB/\Delta$  for loops with  $\Omega = 10, 11, 12, 15, 17.5$ , and 20 are in the tables for  $0 \leq \beta b \leq 2.5$  and for  $0 \leq \frac{\alpha}{\beta} \leq 1$ .

### Graphical Representation

Graphs of the normalized conductance and susceptance of thin-wire loops as a function of the variable  $\beta b = 2\pi b/\lambda$  are shown in Fig. 3-8. The parameter  $a/\beta$  of the surrounding medium ranges from zero to one. Note how insensitive to the size of the loop the admittance becomes as  $a/\beta$  approaches unity. This is true particularly of loops near antiresonance that have a high driving point impedance. Such an insensitivity merely means that most of the current has left the loop and has entered the surrounding dissipative medium.

### Conclusion

The driving-point admittance of bare thin-wire loops  $2 \frac{1}{2}$  wavelengths in circumference when immersed in an arbitrary dissipative medium has been determined from Wu's theory using 20 terms in the Fourier series.

#### LIST OF REFERENCES

1. Hallen, E., "Theoretical Investigations Into Transmitting and Receiving Qualities of Antennae," Nova Acta Regiae Soc. Sci. Upsaliensis [4] 11, 1-44 (1938).
2. Storer, J. E., "Impedance of Thin-Wire Loop Antennas," Trans. Am. Inst. Elec. Engrs. 73, Part I, p. 606 (1956); also Crust Laboratory Technical Report No. 212, May 1, 1955.
3. Wu, T. T., "Theory of Thin Circular Loop Antenna," J. Math. Phys. 3, 1301-1304 (1962).
4. Kraichman, M. B., "Impedance of a Circular Loop in an Infinite Conducting Medium," J. Research Natl. Bur. Standards 66B, pp. 499-503, July-August 1962.
5. Chen, C. L. and King, R. W. P., "The Small Bare Loop Antenna Immersed in a Dissipative Medium," IEEE Trans. AP 11, pp. 266-268, (May 1963).
6. King, R. W. P., "Fundamental Electromagnetic Theory," Appendix II, Dover Publications (1963).
7. Gooch, D. W., Harrison, C. W., Jr., King, R. W. P., and Wu, T. T., "Impedances and Admittances of the Long Antenna in Air and in Dissipative Media With Tables of the Functions  $f(p) \pm ig(p) = \sqrt{1 + ip}$ ," Crust Laboratory Technical Report No. 352, January 15, 1962.
8. Wu, T. T. and King, R. W. P., "Driving Point and Input Admittance of Linear Antennas," J. Appl. Phys. 30, p. 76 (1959).
9. Duncan, R. H. and Hinckley, F. A., "Cylindrical Antenna Theory," J. Research Natl. Bur. Standards 64B, pp. 569-584, September-October 1960.

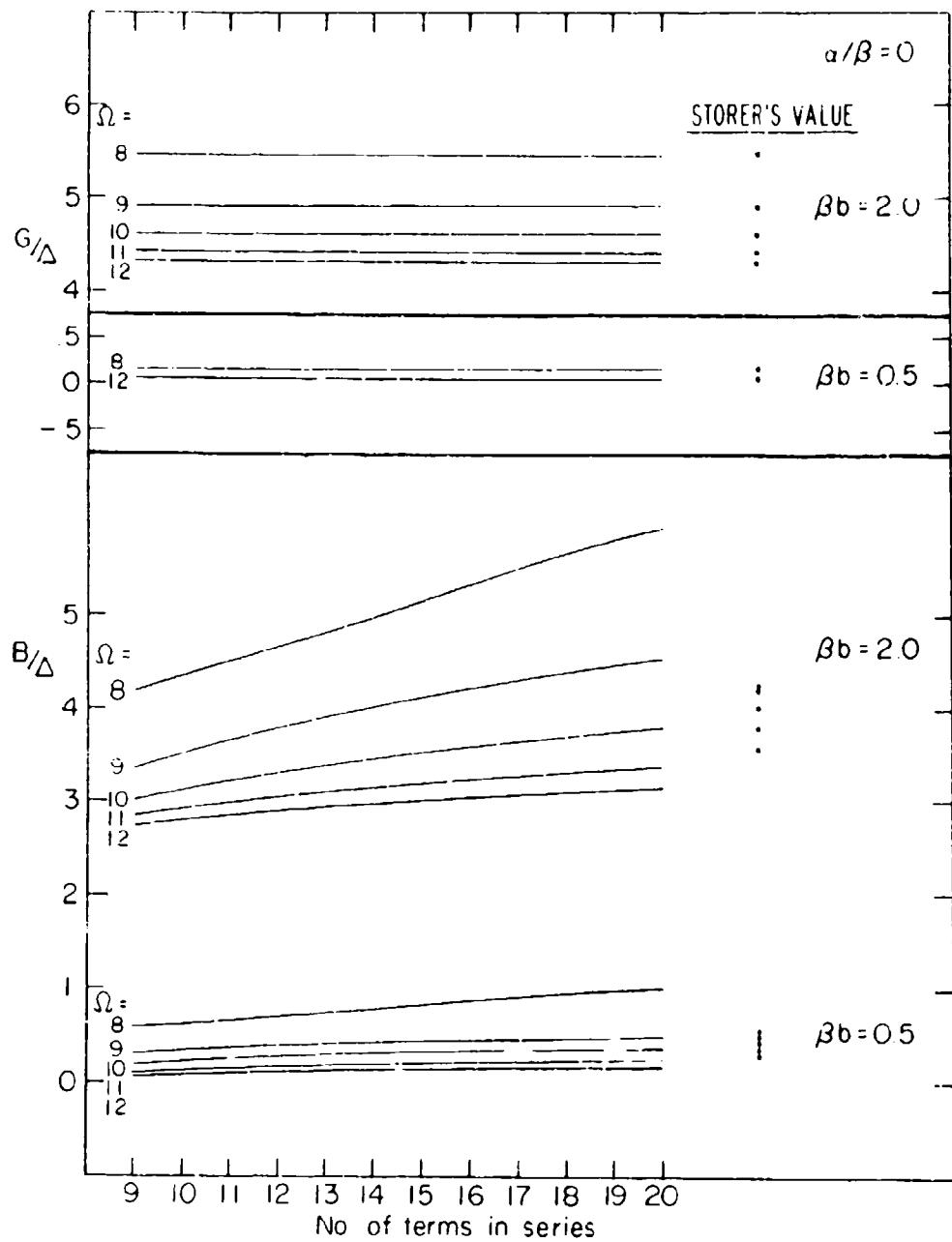


Fig. 1 Normalized conductance and susceptance of circular loop in air as a function of the number of terms - Wu's theory for  $\beta b = 0.5$  and  $2.0$ ,

$$\Omega = 2 \ln\left(\frac{2\pi b}{a}\right) + g - 12$$

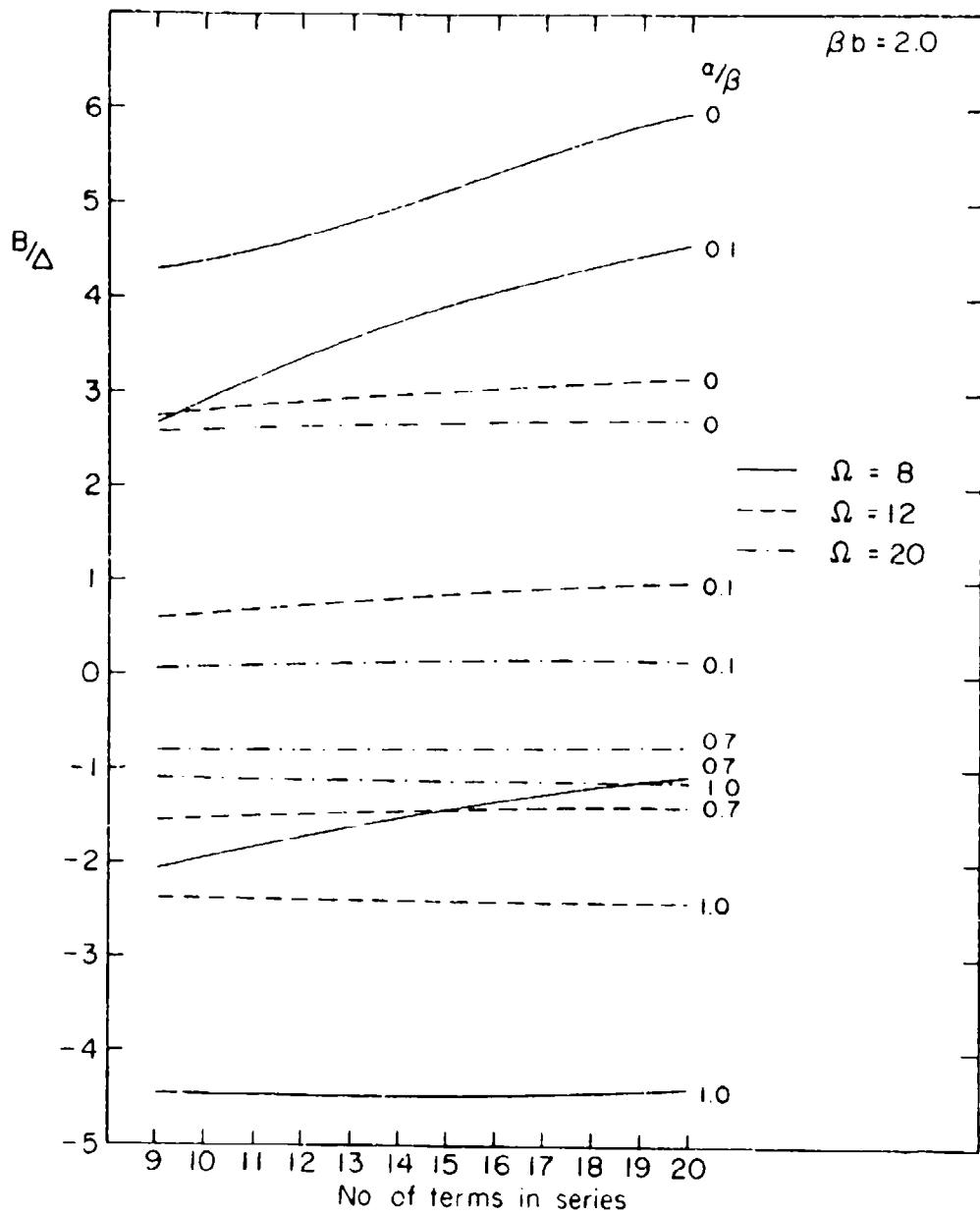


Fig. 2 Normalized susceptance of circular loop in a dissipative medium with propagation constant  $k = \beta - j\alpha$  as a function of the number of terms - Wu's theory for  $\beta b = 2.0$ ,  $\Omega = 8, 12, 20$ ,  $a/\beta = 0 - 1$ .

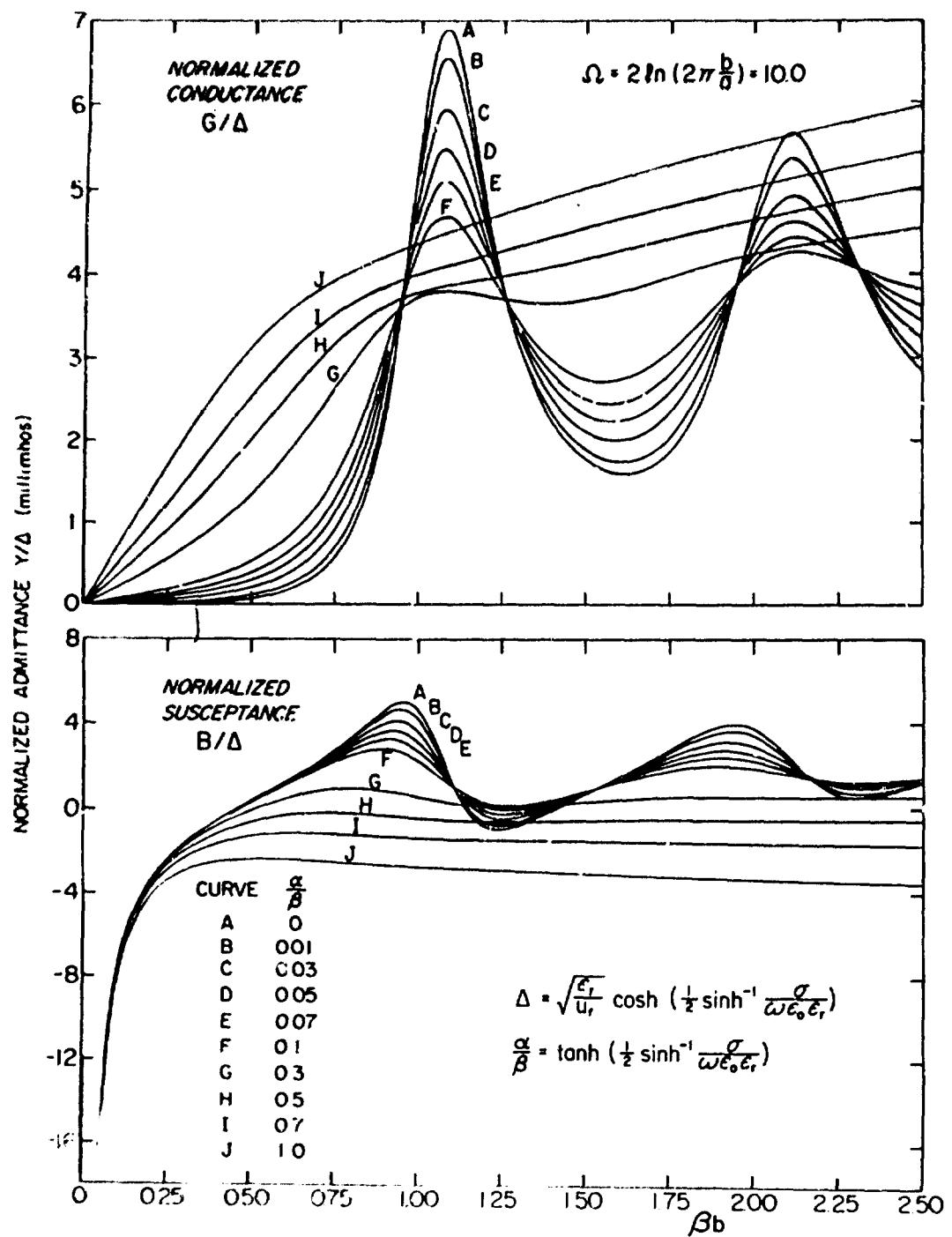


Fig. 3 Normalized admittance of circular loop antenna in a dissipative medium - Wu's theory,  $\Omega = 10$

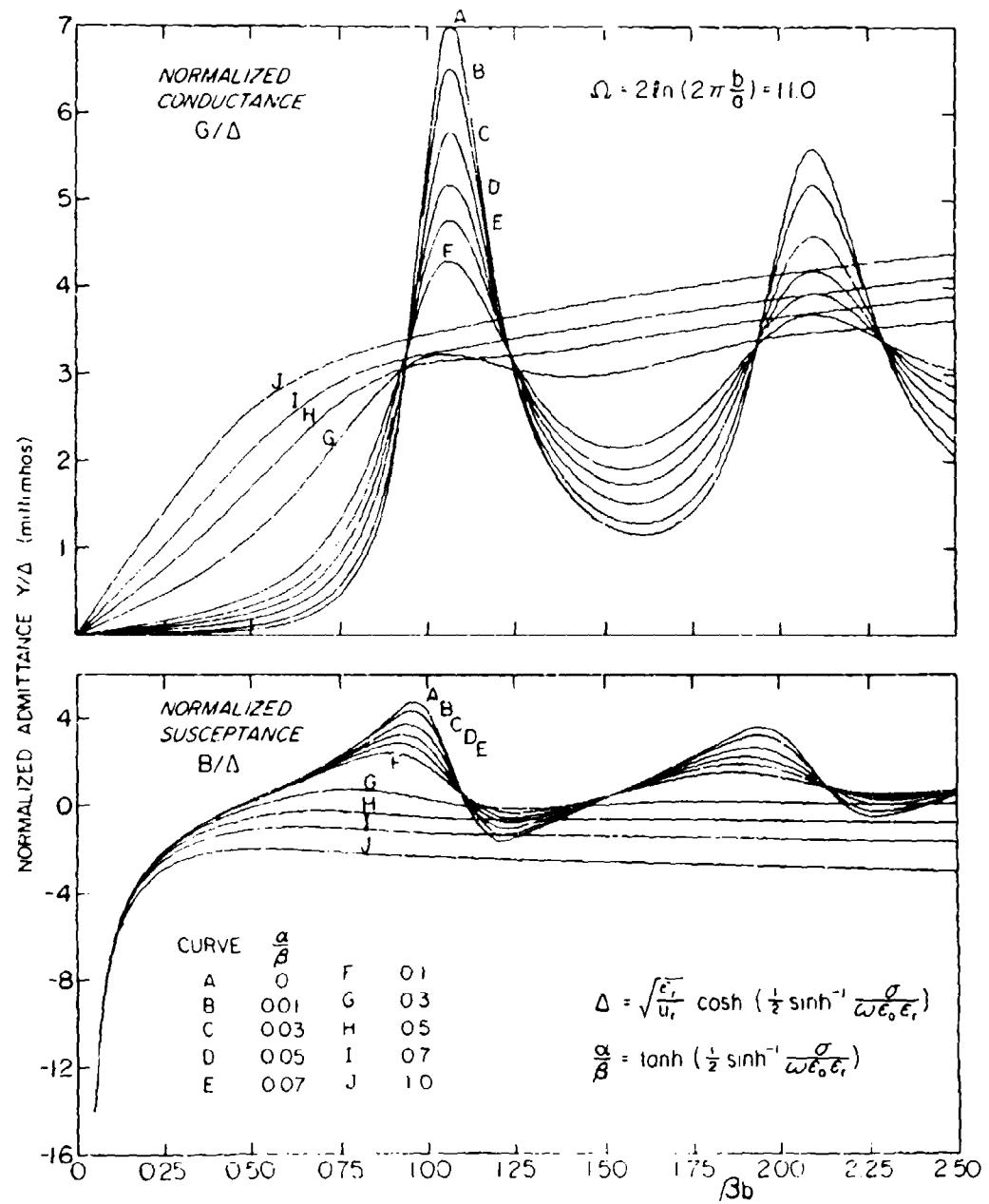


Fig. 4 Normalized admittance of circular loop antenna in a dissipative medium - Wu's theory,  $\Omega = 11$

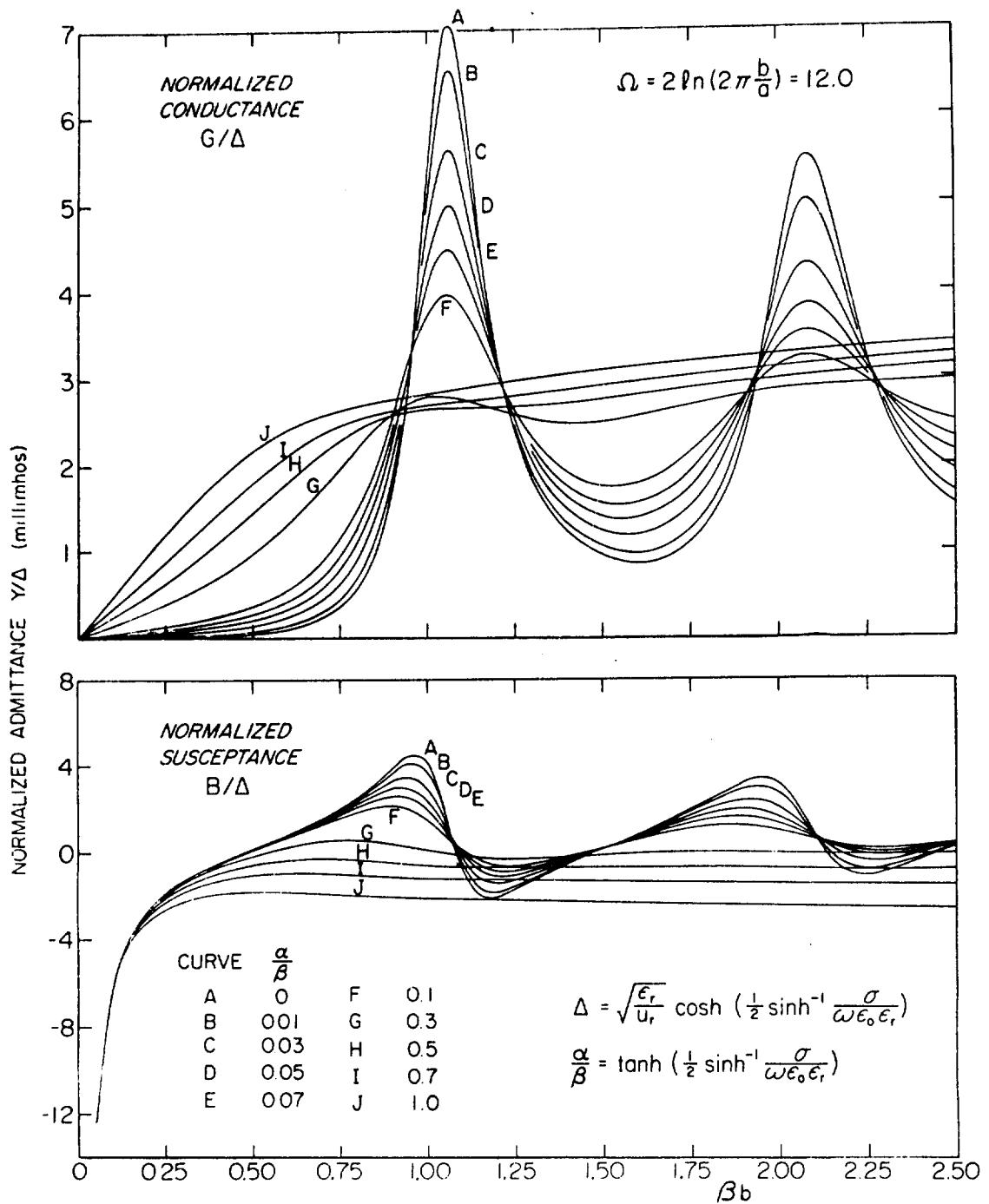


Fig. 5 Normalized admittance of circular loop antenna in a dissipative medium - Wu's theory,  $\Omega = 12$

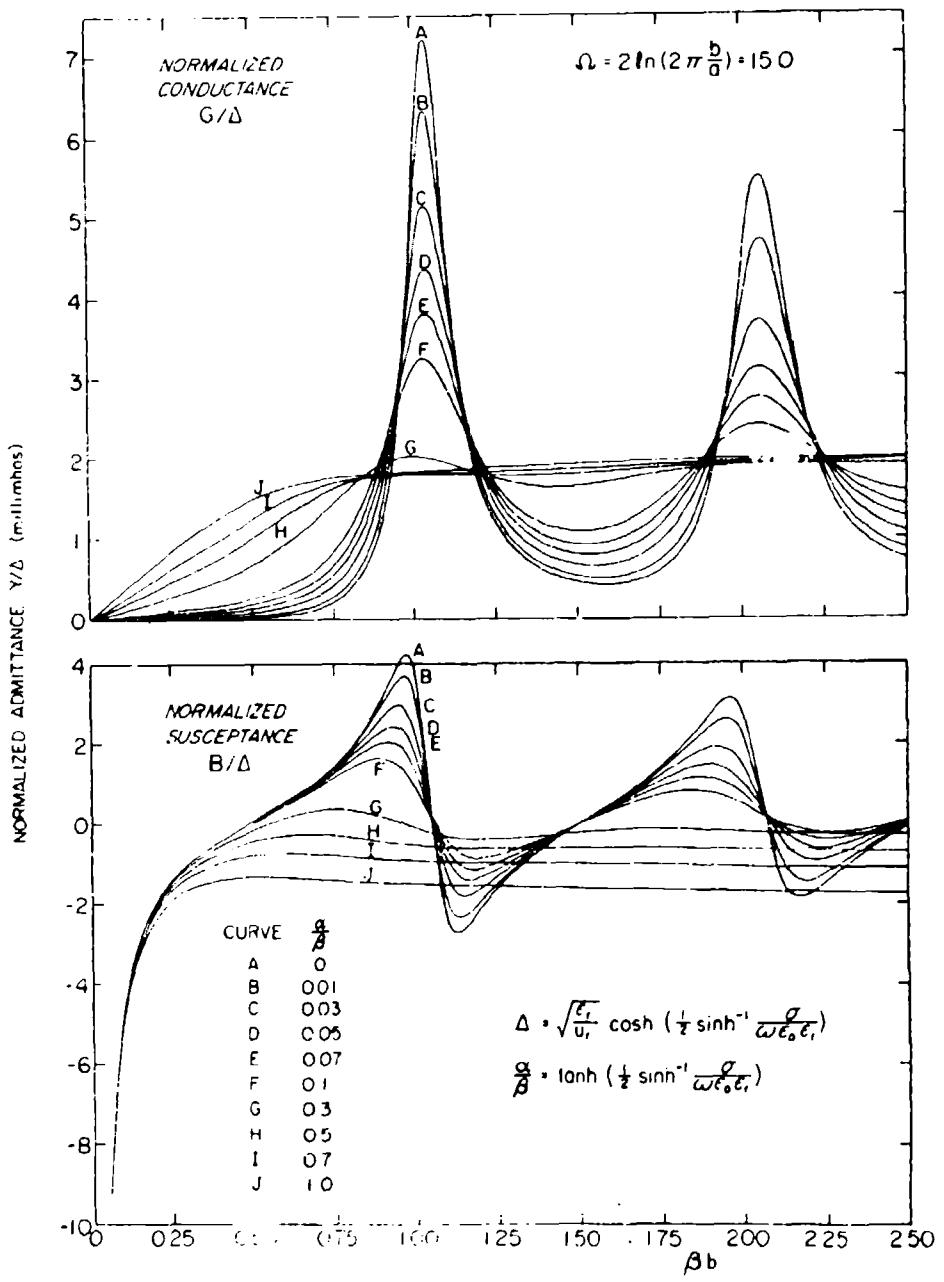


Fig. 6 Normalized admittance of circular loop antenna in a dissipative medium - Wu's theory,  $\Omega = 15$

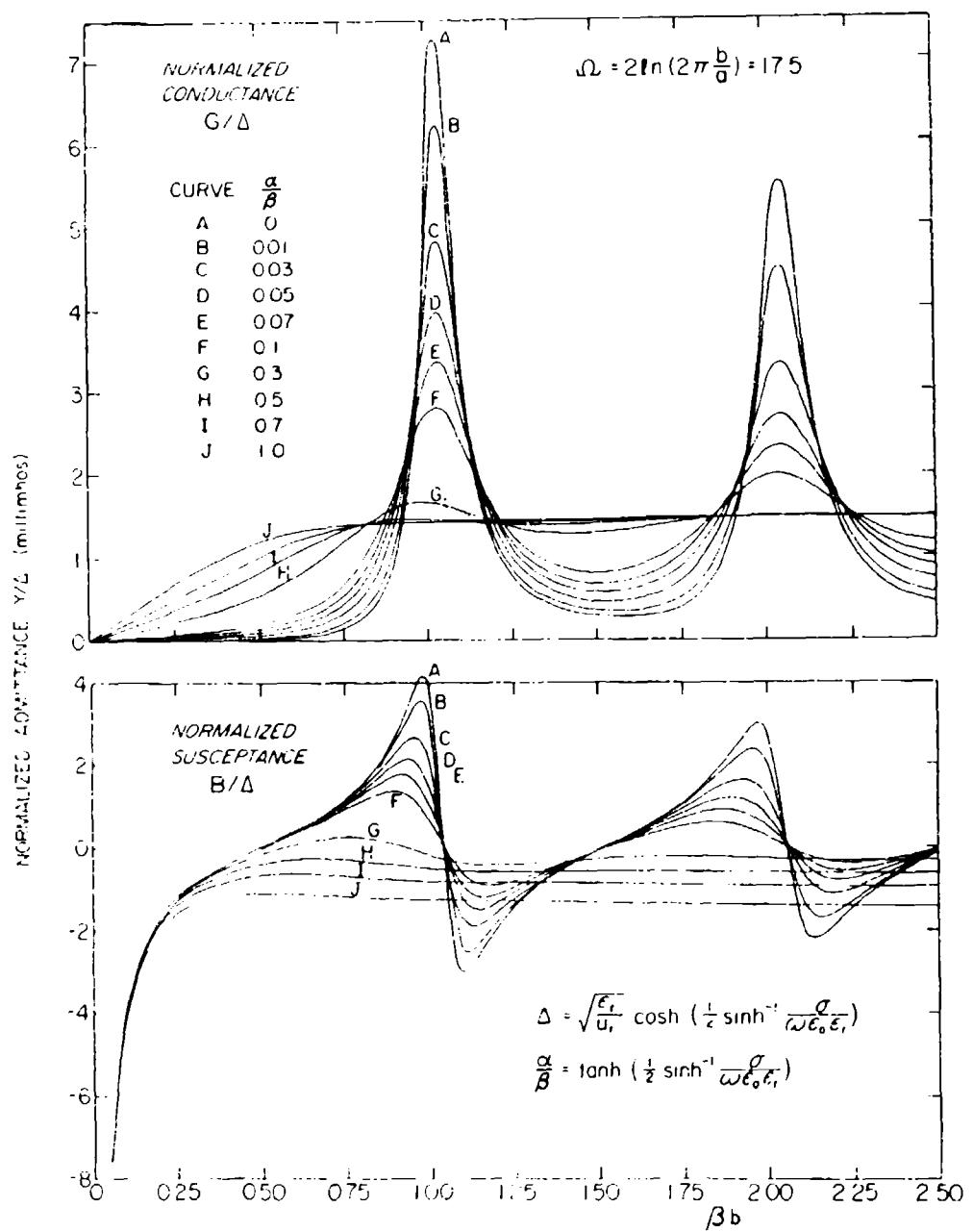


Fig. 7 Normalized admittance of circular loop antenna in a dissipative medium - Wu's theory,  $\Omega = 17.5$

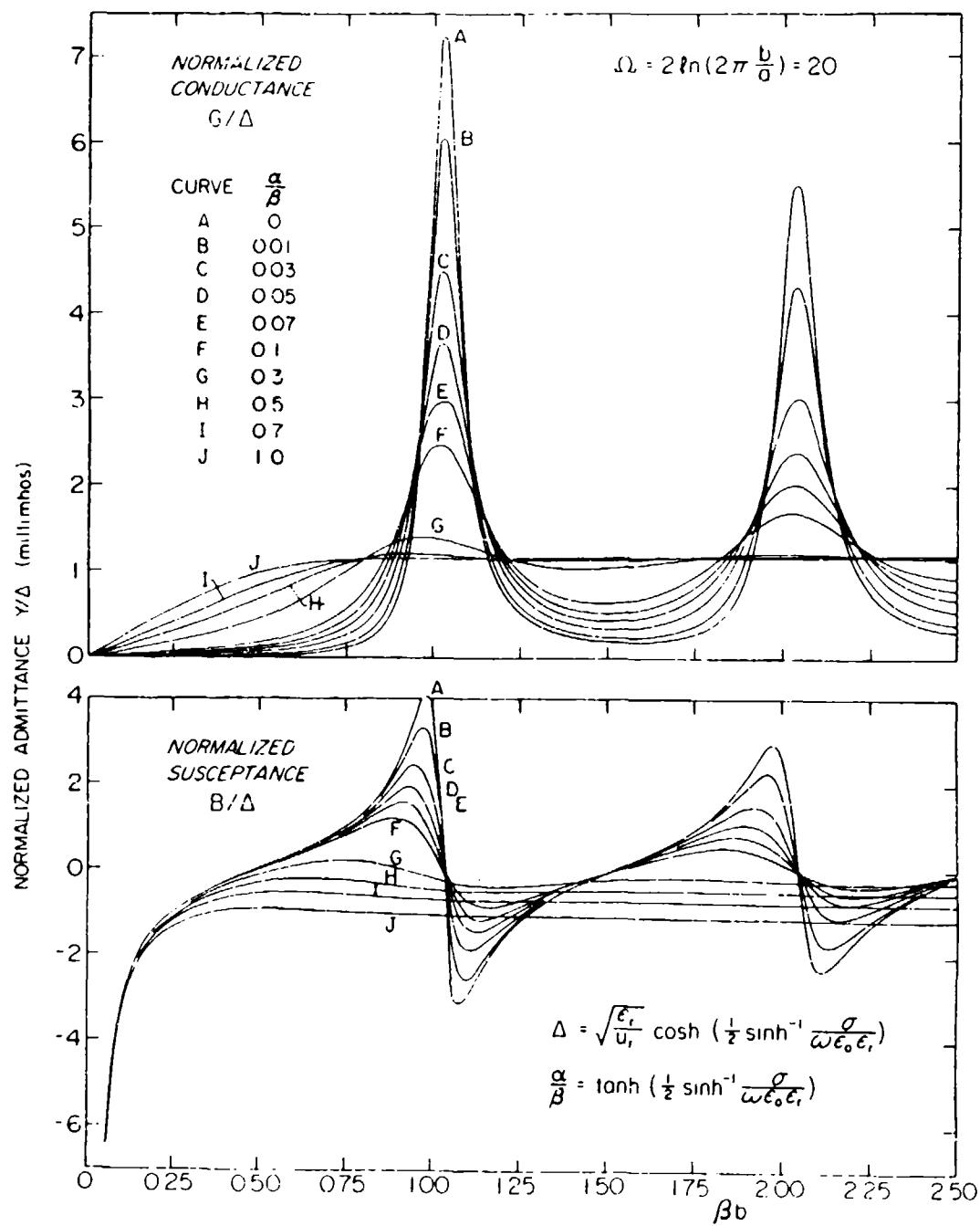


Fig. 8 Normalized admittance of circular loop antenna in a dissipative medium - Wu's theory,  $\Omega = 20$

TABLE I  
Normalized Admittance  $Y/\Delta$  of Loop Antennas in Dissipative Media

$\beta$	$\frac{\alpha}{\beta} = 0.00$			$\frac{\alpha}{\beta} = 0.01$			$\frac{\alpha}{\beta} = 0.03$			$\frac{\alpha}{\beta} = 0.05$			$\frac{\alpha}{\beta} = 0.07$				
	$Y/\Delta$	$Y/\Delta$	$Y/\Delta$	$Y/\Delta$	$Y/\Delta$												
0.05	0.0003	-16.1742	0.0038	-16.1742	0.0108	-16.1744	0.0178	-16.1747	0.0248	-16.1751	0.0507	-7.8257	0.0566	-7.8247	0.0781	-4.9236	
0.10	0.0014	-7.6236	0.0084	-7.8237	0.0225	-7.8241	0.0366	-7.8247	0.0567	-4.9226	0.0567	-4.9226	0.0781	-4.9226	0.1076	-3.3802	
0.15	0.0032	-4.9201	0.0339	-4.9203	0.0353	-4.9209	0.0567	-4.9209	0.0787	-3.3779	0.0787	-3.3779	0.1076	-3.3779	0.1401	-2.3767	
0.20	0.0061	-3.3750	0.0206	-3.3752	0.0496	-3.3763	0.0787	-3.3779	0.1076	-3.3802	0.1076	-3.3802	0.1401	-2.3767	0.1766	-1.6391	
0.25	0.0102	-2.3691	0.0686	-2.3696	0.0660	-2.3711	0.1031	-2.3735	0.1401	-2.3767	0.1031	-2.3735	0.1766	-1.6391	0.2186	-1.0487	
0.30	0.0162	-1.6283	0.0592	-1.6290	0.0851	-1.6313	0.1309	-1.6346	0.1766	-1.6391	0.1309	-1.6346	0.2186	-1.0487	0.2680	-0.5452	
0.35	0.0242	-1.0333	0.0526	-1.0345	0.1081	-1.0378	0.1634	-1.0426	0.2186	-1.0487	0.1081	-1.0426	0.2680	-0.5452	0.3938	-0.0938	
0.40	0.0370	-0.5233	0.0702	-0.5250	0.1504	-0.5300	0.2024	-0.5367	0.3276	-0.5452	0.1504	-0.5367	0.3938	-0.0938	0.4013	0.3274	
0.45	0.0546	-0.0624	0.0939	-0.0951	0.1723	-0.0723	0.2502	-0.0819	0.3276	-0.0938	0.1723	-0.0819	0.3938	-0.0938	0.4013	0.3274	
0.50	0.0801	0.3730	0.1266	0.3688	0.2191	0.3580	0.3107	0.3442	0.4013	0.3274	0.2191	0.3580	0.3938	-0.0938	0.4013	0.3274	
0.55	0.1174	0.8096	0.1724	0.7939	0.2814	0.7776	0.3839	0.7574	0.4947	0.7335	0.2814	0.7776	0.3839	0.7574	0.4947	0.7335	
0.60	0.1728	1.2351	0.2380	1.2247	0.3666	1.1997	0.4926	1.1698	0.6158	1.1350	0.3666	1.1997	0.4926	1.1698	0.6158	1.1350	
0.65	0.2561	1.6908	0.3337	1.6740	0.4957	1.6354	0.6333	1.5903	0.7761	1.5393	0.4957	1.6354	0.6333	1.5903	0.7761	1.5393	
0.70	0.3837	2.1816	0.4765	2.1545	0.6563	2.0937	0.8252	2.0249	0.9491	1.9491	0.6563	2.0937	0.8252	2.0249	0.9491	1.9491	
0.75	0.5830	2.7214	0.6938	2.6768	0.951	2.5796	1.1~27	2.4733	2.3599	2.3599	0.951	2.5796	1.1~27	2.4733	2.3599	2.3599	
0.80	0.9009	3.3195	1.0313	3.2450	1.2738	3.0977	1.4249	1.9229	1.6899	2.7536	1.0313	3.2450	1.2738	1.9229	1.6899	2.7536	
0.85	1.4151	3.9671	1.5620	3.8414	1.8222	3.5873	2.0441	3.3345	2.2330	3.0870	1.5620	3.8414	1.8222	3.3345	2.2330	3.0870	
0.90	2.2513	4.5965	2.3902	4.3886	2.6194	3.9208	2.7957	3.6205	2.9313	3.2790	2.3902	4.3886	2.6194	3.6205	2.9313	3.2790	
0.95	3.5409	4.9903	3.6073	4.6755	3.6909	4.1131	3.7295	3.6295	3.7408	3.2122	3.6073	4.1131	3.7295	3.6295	3.7408	3.2122	
1.00	5.2227	4.6875	5.1043	4.3157	4.8814	3.6941	4.6628	3.1964	4.5101	2.7892	4.0013	4.6628	3.1964	4.5101	2.7892	4.0013	
1.05	6.6359	3.2896	6.3011	3.0661	5.7564	2.6416	5.3366	2.3176	5.0076	2.0532	5.0076	2.6416	5.3366	2.3176	5.0076	2.0532	
1.10	6.8730	1.3221	5.5054	1.3362	5.9058	1.3233	5.4445	1.2783	5.0849	1.2165	5.0849	1.3233	5.4445	1.2783	5.0849	1.2165	
1.15	6.0398	-0.1400	5.6108	0.0327	5.4080	0.2831	5.0746	0.4422	4.8014	0.5392	4.8014	0.2831	5.0746	0.4422	4.8014	0.5392	
1.20	4.9127	-0.7848	4.8271	-0.5974	4.6528	-0.2698	4.4874	-0.0365	4.3390	0.1313	4.3390	-0.2698	4.4874	-0.0365	4.3390	0.1313	
1.25	3.9355	-0.8825	3.9255	3.9399	-0.7158	3.9256	-0.4304	3.9932	-0.2040	3.8535	-0.0287	3.8535	-0.4304	3.9932	-0.2040	3.8535	-0.0287
1.30	3.1945	-0.7081	3.2478	-0.5803	3.3294	-0.1531	3.3957	-0.1640	3.4253	-0.0112	3.4253	-0.1531	3.3957	-0.1640	3.4253	-0.0112	
1.35	2.6537	-0.4132	2.7340	-0.3195	2.8724	-0.1475	2.9866	-0.0316	3.0804	0.1186	3.0804	-0.1475	2.9866	-0.0316	3.0804	0.1186	
1.40	2.2627	-0.0671	2.3595	0.0908	2.5343	0.1243	2.6865	0.2295	2.8192	0.3155	2.8192	0.1243	2.6865	0.2295	2.8192	0.3155	
1.45	1.9826	0.3014	2.0916	0.3479	2.2929	0.4306	2.4731	0.4985	2.6341	0.5512	2.6341	0.4306	2.4731	0.4985	2.6341	0.5512	
1.50	1.7878	0.6819	1.9076	0.7098	2.1311	0.7558	2.5358	0.7885	2.5167	0.8682	2.5167	0.7558	2.5358	0.7885	2.5167	0.8682	
1.55	1.6637	1.0722	1.7942	1.0822	2.0383	1.0923	2.2603	1.0898	2.4608	1.0758	2.4608	1.0923	2.2603	1.0898	2.4608	1.0758	
1.60	1.6039	1.4734	1.7457	1.4644	2.0098	1.4359	2.2484	1.3956	2.4626	1.3455	2.4626	1.4359	2.2484	1.3956	2.4626	1.3455	
1.65	1.6093	1.8871	1.7628	1.8558	2.0457	1.7829	2.2976	1.6996	2.5206	1.6099	2.5206	1.7829	2.2976	1.6996	2.5206	1.6099	
1.70	1.6877	2.3137	1.8524	2.2545	2.1504	2.1276	2.4098	1.9945	2.6346	1.8597	2.6346	2.1504	2.1276	2.4098	1.9945	2.6346	
1.75	1.8540	2.7491	2.0269	2.6535	2.3315	2.4594	2.5880	2.2679	2.0835	2.2679	2.0835	2.6535	2.3315	2.4594	2.5880	2.2679	
1.80	2.1306	3.1797	2.3038	3.0368	2.5975	2.7605	2.8540	2.5028	3.0263	2.2684	3.0263	2.7605	2.8540	2.5028	3.0263	2.2684	
1.85	2.5444	3.5744	2.7011	3.3725	2.9531	3.0230	3.1440	2.6759	3.2927	2.3907	3.2927	3.0230	3.1440	2.6759	3.2927	2.3907	
1.90	3.1165	3.2271	3.6268	3.3902	3.3902	3.5030	3.7596	3.1316	3.5864	2.4389	3.5864	3.3902	3.7596	3.1316	3.5864	2.4389	
1.95	3.8359	3.9815	3.8587	3.6637	3.8765	3.4006	3.8793	2.7291	3.802	2.3989	3.802	3.4006	3.8793	2.7291	3.802	2.3989	
2.00	4.6171	3.7906	4.5146	3.4690	4.3470	2.9598	4.2248	2.5745	4.1397	2.2712	4.1397	2.9598	4.2248	2.5745	4.1397	2.2712	
2.05	5.2801	3.2530	5.0531	3.0048	5.7145	2.6125	4.4854	2.3133	4.3399	2.0738	4.3399	2.6125	4.4854	2.3133	4.3399	2.0738	
2.10	5.6233	2.4710	5.3316	2.3600	4.9046	2.1627	4.6209	1.9919	4.4316	1.8404	4.4316	2.1627	4.6209	1.9919	4.4316	1.8404	
2.15	5.5686	1.6718	5.2987	1.7930	4.8948	1.7088	4.6219	1.6713	4.4387	1.6107	4.4387	1.7088	4.6219	1.6713	4.4387	1.6107	
2.20	5.2098	1.0560	5.0200	1.1830	4.7214	1.3374	4.5110	1.4348	4.3674	1.4188	4.3674	1.3374	4.5110	1.4348	4.3674	1.4188	
2.25	4.7102	0.6964	4.6146	0.8631	4.4510	1.0927	4.3285	1.2227	4.2438	1.2853	4.2438	1.0927	4.3285	1.2227	4.2438	1.2853	
2.30	4.1983	0.5656	4.1341	0.7327	4.1477	0.9786	4.1155	1.1316	4.0952	1.2167	4.0952	0.9786	4.1155	1.1316	4.0952	1.2167	
2.35	3.7412	0.6027	3.7886	0.7500	3.8563	0.9755	3.9044	1.1231	3.9448	1.2091	3.9448	0.9755	3.9044	1.1231	3.9448	1.2091	
2.40	3.3624	0.7520	3.4543	0.8714	3.6021	1.0578	3.7163	1.1816	3.8092	1.2532	3.8092	1.0578	3.7163	1.1816	3.8092	1.2532	
2.45	3.0648	0.9739	3.1888	1.0632	3.3970	1.2017	3.5633	1.2908	3.6990	1.3574	3.6990	1.0632	3.3970	1.2908	3.6990	1.3574	
2.50	2.8436	1.2429	2.9916	1.3016	3.2453	1.3380	3.4505	1.4360	3.6204	1.4506	3.6204	1.3380	3.4505	1.4360	3.6204	1.4506	

TABLE I  
Normalized Admittance Y/Δ of Loop Antennas in Dissipative Media

$\beta c$	$\frac{\alpha}{\beta} = 0.10$	$\Omega = 10$			$\Omega = 10$					
		$\frac{\alpha}{\beta} = 0.30$	$\frac{\alpha}{\beta} = 0.50$	$\frac{\alpha}{\beta} = 0.70$	$\frac{\alpha}{\beta} = 0.30$	$\frac{\alpha}{\beta} = 0.50$	$\frac{\alpha}{\beta} = 0.70$			
0.05	0.0353	-16.1760	0.1052	0.16.1903	0.1750	-16.2186	0.2446	-16.2609	0.3485	-16.3505
0.10	0.0718	-7.8276	0.2123	-7.8572	0.3520	-7.9152	0.4905	-8.0016	0.6954	-8.1837
0.15	0.1102	-4.9267	0.3228	-4.9733	0.5328	-5.0639	0.7392	-5.1977	1.0399	-5.4773
0.20	0.1511	-3.3848	0.4382	-3.4511	0.7192	-3.5784	0.9916	-3.7645	1.3802	-4.1492
0.25	0.1956	-2.3831	0.5604	-2.4731	0.9127	-2.6427	1.2483	-2.8872	1.7135	-3.3821
0.30	0.2450	-1.6478	0.6914	-1.7670	1.1449	-1.9863	1.5087	-2.2964	2.0360	-2.9087
0.35	0.3009	-1.0606	0.8334	-1.2165	1.3268	-1.4950	1.7717	-1.8784	2.3432	-2.6117
0.40	0.3657	-0.5613	0.9892	-0.7645	1.5488	-1.1134	2.0348	-1.5774	2.6307	-2.4314
0.45	0.4424	-0.1159	1.1614	-0.3906	1.7806	-0.8128	2.2946	-1.3632	2.8944	-2.3322
0.50	0.5353	0.2969	1.3530	-0.0485	2.0207	-0.5776	2.5466	-1.2173	3.1316	-2.2904
0.55	0.6501	0.6208	1.5664	0.2395	2.2659	-0.3994	2.7858	-1.1265	3.3411	-2.2880
0.60	0.7951	1.0747	1.8033	0.4953	2.5114	-0.2731	3.076	-1.0804	3.5237	-2.3117
0.65	0.9811	1.4529	2.0634	0.6864	2.7509	-0.1947	3.2678	-1.0692	3.6816	-2.3511
0.70	1.2227	1.8246	2.3432	0.8372	2.9772	-0.1596	3.3840	-1.0835	3.8180	-2.3985
0.75	1.5384	2.1802	2.6350	0.9311	3.1830	-0.1616	3.5356	-1.147	3.9368	-2.4487
0.80	1.9479	2.4969	2.9256	0.9628	3.3624	-0.1923	3.6639	-1.1552	4.0416	-2.4985
0.85	2.4647	2.7317	3.1976	0.9319	3.5120	-0.2425	3.7715	-1.1986	4.1557	-2.5462
0.90	3.0788	2.8191	3.4323	0.8458	3.6316	-0.3021	3.8622	-1.2408	4.2219	-2.5909
0.95	3.7301	2.6862	3.6142	0.7204	3.7235	-0.3628	3.9396	-1.2788	4.3023	-2.6327
1.00	4.2963	2.2997	3.7357	0.5770	3.7927	-0.4177	4.0076	-1.3114	4.3784	-2.6718
1.05	4.6365	1.7229	3.7992	0.4377	3.8447	-0.4527	4.0692	-1.3384	4.4513	-2.7087
1.10	4.6827	1.1086	3.8155	0.3199	3.8853	-0.4961	4.1269	-1.3602	4.5218	-2.7437
1.15	4.4843	0.6080	3.7994	0.2339	3.9197	-0.5179	4.1823	-1.3779	4.5902	-2.7774
1.20	4.1542	0.2923	3.7664	0.1828	3.9519	-0.5295	4.2367	-1.3923	4.6568	-2.8099
1.25	3.7946	0.1555	3.7293	0.1544	3.9846	-0.5328	4.2907	-1.4044	4.7218	-2.8417
1.30	3.4663	0.1568	3.6975	0.1731	4.0195	-0.5302	4.3446	-1.4152	4.7852	-2.8728
1.35	3.1955	0.2528	3.6769	0.2024	4.0575	-0.5238	4.3983	-1.4251	4.8472	-2.9034
1.40	2.9886	0.4096	3.6706	0.2454	4.0987	-0.5153	4.4519	-1.4348	4.9077	-2.9336
1.45	2.8440	0.6017	3.6795	0.2962	4.1428	-0.5064	4.5051	-1.4446	4.9669	-2.9633
1.50	2.7573	0.8144	3.7030	0.3496	4.1893	-0.4981	4.5578	-1.4546	5.0246	-2.9927
1.55	2.7244	1.0356	3.7396	0.4014	4.2373	-0.4911	4.6098	-1.4650	5.0811	-3.0217
1.60	2.7418	1.2561	3.7869	0.4484	4.2862	-0.4958	4.6609	-1.4757	5.1363	-3.0503
1.65	2.8070	1.4673	3.8422	0.4885	4.3352	-0.4823	4.7111	-1.4866	5.1903	-3.0765
1.70	2.9171	1.6602	3.9028	0.5203	4.3837	-0.4806	4.7602	-1.4979	5.2431	-3.1064
1.75	3.0684	1.8250	3.9657	0.5434	4.4315	-0.4804	4.8094	-1.5092	5.2949	-3.1339
1.80	3.2541	1.9509	4.0284	0.5582	4.4780	-0.4815	4.8555	-1.5207	5.3455	-3.1610
1.85	3.4638	2.0275	4.0887	0.5656	4.5232	-0.4835	4.9017	-1.5322	5.3952	-3.1878
1.90	3.6820	2.0471	4.1451	0.5671	4.5671	-0.4861	4.9469	-1.5438	5.4438	-3.2142
1.95	3.8893	2.0078	4.1964	0.5645	4.6096	-0.4891	4.9913	-1.5552	5.4916	-3.2403
2.00	4.0653	1.9156	4.2423	0.5594	4.6509	-0.4922	5.0348	-1.5667	5.5384	-3.2661
2.05	4.1927	1.7855	4.2829	0.5537	4.6910	-0.4953	5.0775	-1.5780	5.5844	-3.2915
2.10	4.2625	1.6384	4.3189	0.5486	4.7302	-0.4983	5.1194	-1.5893	5.6295	-3.3166
2.15	4.2753	1.4968	4.3510	0.5451	4.7685	-0.5012	5.1606	-1.6005	5.6739	-3.3414
2.20	4.2408	1.3793	4.3804	0.5440	4.8062	-0.5039	5.2012	-1.6116	5.7174	-3.3659
2.25	4.1736	1.2975	4.4080	0.5453	4.8433	-0.5065	5.2411	-1.6227	5.7602	-3.3900
2.30	4.0996	1.2560	4.4349	0.5491	4.8799	-0.5089	5.2804	-1.6337	5.8023	-3.4139
2.35	4.0029	1.2535	4.4617	0.5551	4.9160	-0.5114	5.3190	-1.6447	5.8437	-3.4375
2.40	3.9247	1.2851	4.4891	0.5628	4.9517	-0.5138	5.3571	-1.6556	5.8844	-3.4607
2.45	3.8627	1.3440	4.5175	0.5717	4.9870	-0.5163	5.3945	-1.6665	5.9245	-3.4837
2.50	3.8218	1.4225	4.5471	0.5811	5.0219	-0.5188	5.4315	-1.6773	5.9639	-3.5064

TABLE II  
Normalized Admittance  $Y/\Delta$  of Loop Antennas in Dissipative Media

$\frac{\sigma}{\beta}$	$\frac{\sigma}{\beta} = 0.00$						$\frac{\sigma}{\beta} = 0.01$						$\frac{\sigma}{\beta} = 0.03$						$\frac{\sigma}{\beta} = 0.05$						$\frac{\sigma}{\beta} = 0.07$							
	$Y/\Delta$			$Y/\Delta$			$Y/\Delta$			$Y/\Delta$			$Y/\Delta$			$Y/\Delta$			$Y/\Delta$			$Y/\Delta$			$Y/\Delta$			$Y/\Delta$				
0.05	0.0032	-14.0300	0.0031	-14.0300	0.0089	-14.0302	0.5446	-14.0304	0.0204	-14.0308	0.0300	-6.7938	0.0300	-6.7933	0.0416	-6.5001	0.0416	-6.5001	0.0416	-6.5001	0.0416	-6.5001	0.0416	-6.5001	0.0416	-6.5001	0.0416	-6.5001	0.0416	-6.5001		
0.10	0.0010	-6.7984	0.0068	-6.7985	0.0184	-6.7985	0.0300	-6.7985	0.0300	-6.7985	0.0300	-6.7985	0.0300	-6.7985	0.0300	-6.7985	0.0300	-6.7985	0.0300	-6.7985	0.0300	-6.7985	0.0300	-6.7985	0.0300	-6.7985	0.0300	-6.7985	0.0300	-6.7985		
0.15	0.0024	-4.2391	0.0112	-4.2392	0.0289	-4.2392	0.0465	-4.2392	0.0465	-4.2392	0.0465	-4.2392	0.0465	-4.2392	0.0465	-4.2392	0.0465	-4.2392	0.0465	-4.2392	0.0465	-4.2392	0.0465	-4.2392	0.0465	-4.2392	0.0465	-4.2392	0.0465	-4.2392		
0.20	0.0046	-2.9573	0.0165	-2.9576	0.0405	-2.9584	0.0644	-2.9584	0.0644	-2.9584	0.0644	-2.9584	0.0644	-2.9584	0.0644	-2.9584	0.0644	-2.9584	0.0644	-2.9584	0.0644	-2.9584	0.0644	-2.9584	0.0644	-2.9584	0.0644	-2.9584	0.0644	-2.9584		
0.25	0.0077	-2.0031	0.0230	-2.0035	0.0537	-2.0047	0.0843	-2.0047	0.0843	-2.0047	0.0843	-2.0047	0.0843	-2.0047	0.0843	-2.0047	0.0843	-2.0047	0.0843	-2.0047	0.0843	-2.0047	0.0843	-2.0047	0.0843	-2.0047	0.0843	-2.0047	0.0843	-2.0047		
0.30	0.0122	-1.4685	0.0312	-1.4591	0.0692	-1.4639	0.1071	-1.4639	0.1071	-1.4639	0.1071	-1.4639	0.1071	-1.4639	0.1071	-1.4639	0.1071	-1.4639	0.1071	-1.4639	0.1071	-1.4639	0.1071	-1.4639	0.1071	-1.4639	0.1071	-1.4639	0.1071	-1.4639		
0.35	0.0197	-0.9503	0.0417	-0.9517	0.0877	-0.9538	0.1336	-0.9538	0.1336	-0.9538	0.1336	-0.9538	0.1336	-0.9538	0.1336	-0.9538	0.1336	-0.9538	0.1336	-0.9538	0.1336	-0.9538	0.1336	-0.9538	0.1336	-0.9538	0.1336	-0.9538	0.1336	-0.9538		
0.40	0.0279	-0.5154	0.0555	-0.5168	0.1106	-0.5207	0.1654	-0.5207	0.1654	-0.5207	0.1654	-0.5207	0.1654	-0.5207	0.1654	-0.5207	0.1654	-0.5207	0.1654	-0.5207	0.1654	-0.5207	0.1654	-0.5207	0.1654	-0.5207	0.1654	-0.5207	0.1654	-0.5207		
0.45	0.0413	-0.1228	0.0741	-0.1249	0.1395	-0.1306	0.2645	-0.1306	0.2645	-0.1306	0.2645	-0.1306	0.2645	-0.1306	0.2645	-0.1306	0.2645	-0.1306	0.2645	-0.1306	0.2645	-0.1306	0.2645	-0.1306	0.2645	-0.1306	0.2645	-0.1306	0.2645			
0.50	0.0606	0.2483	0.0996	0.2450	0.1771	0.2365	0.2540	0.2365	0.2540	0.2365	0.2540	0.2365	0.2540	0.2365	0.2540	0.2365	0.2540	0.2365	0.2540	0.2365	0.2540	0.2365	0.2540	0.2365	0.2540	0.2365	0.2540	0.2365	0.2540			
0.55	0.0890	0.6135	0.1354	0.6084	0.2274	0.5955	0.3181	0.5955	0.3181	0.5955	0.3181	0.5955	0.3181	0.5955	0.3181	0.5955	0.3181	0.5955	0.3181	0.5955	0.3181	0.5955	0.3181	0.5955	0.3181	0.5955	0.3181	0.5955	0.3181	0.5955		
0.60	0.1314	0.9667	0.1869	0.9785	0.2963	0.5878	0.4036	0.5878	0.4036	0.5878	0.4036	0.5878	0.4036	0.5878	0.4036	0.5878	0.4036	0.5878	0.4036	0.5878	0.4036	0.5878	0.4036	0.5878	0.4036	0.5878	0.4036	0.5878	0.4036	0.5878		
0.65	0.1958	1.3913	0.2625	1.3682	0.3934	1.3372	0.5206	1.3372	0.5206	1.3372	0.5206	1.3372	0.5206	1.3372	0.5206	1.3372	0.5206	1.3372	0.5206	1.3372	0.5206	1.3372	0.5206	1.3372	0.5206	1.3372	0.5206	1.3372	0.5206	1.3372		
0.70	0.2957	1.6124	0.3767	1.7908	0.5341	1.7613	0.6847	1.7613	0.6847	1.7613	0.6847	1.7613	0.6847	1.7613	0.6847	1.7613	0.6847	1.7613	0.6847	1.7613	0.6847	1.7613	0.6847	1.7613	0.6847	1.7613	0.6847	1.7613	0.6847	1.7613		
0.75	0.4550	2.2969	0.5541	2.2605	0.7434	2.1795	0.9205	2.1795	0.9205	2.1795	0.9205	2.1795	0.9205	2.1795	0.9205	2.1795	0.9205	2.1795	0.9205	2.1795	0.9205	2.1795	0.9205	2.1795	0.9205	2.1795	0.9205	2.1795	0.9205	2.1795		
0.80	0.7169	2.9520	0.8379	2.7992	1.0628	2.6537	1.2655	2.6537	1.2655	2.6537	1.2655	2.6537	1.2655	2.6537	1.2655	2.6537	1.2655	2.6537	1.2655	2.6537	1.2655	2.6537	1.2655	2.6537	1.2655	2.6537	1.2655	2.6537	1.2655	2.6537		
0.85	1.1622	3.1622	1.4865	3.0522	1.5590	3.1444	1.7332	3.1444	1.7332	3.1444	1.7332	3.1444	1.7332	3.1444	1.7332	3.1444	1.7332	3.1444	1.7332	3.1444	1.7332	3.1444	1.7332	3.1444	1.7332	3.1444	1.7332	3.1444	1.7332	3.1444		
0.90	1.9371	4.1612	2.0856	3.9612	2.3258	3.5737	2.5642	3.5737	2.5642	3.5737	2.5642	3.5737	2.5642	3.5737	2.5642	3.5737	2.5642	3.5737	2.5642	3.5737	2.5642	3.5737	2.5642	3.5737	2.5642	3.5737	2.5642	3.5737	2.5642	3.5737		
0.95	3.2622	4.6662	3.4333	4.3304	4.3364	3.7337	4.4678	3.7337	4.4678	3.7337	4.4678	3.7337	4.4678	3.7337	4.4678	3.7337	4.4678	3.7337	4.4678	3.7337	4.4678	3.7337	4.4678	3.7337	4.4678	3.7337	4.4678	3.7337	4.4678	3.7337	4.4678	
1.00	5.1932	4.2834	5.0403	3.9540	3.9540	4.7489	3.2605	4.7489	3.2605	4.7489	3.2605	4.7489	3.2605	4.7489	3.2605	4.7489	3.2605	4.7489	3.2605	4.7489	3.2605	4.7489	3.2605	4.7489	3.2605	4.7489	3.2605	4.7489	3.2605	4.7489		
1.05	6.8232	2.5879	6.3748	2.3552	2.3552	5.6666	1.9755	5.6666	1.9755	5.6666	1.9755	5.6666	1.9755	5.6666	1.9755	5.6666	1.9755	5.6666	1.9755	5.6666	1.9755	5.6666	1.9755	5.6666	1.9755	5.6666	1.9755	5.6666	1.9755	5.6666		
1.10	6.7120	0.1631	6.2925	0.2928	5.6112	0.4414	5.6112	0.4414	5.6112	0.4414	5.6112	0.4414	5.6112	0.4414	5.6112	0.4414	5.6112	0.4414	5.6112	0.4414	5.6112	0.4414	5.6112	0.4414	5.6112	0.4414	5.6112	0.4414	5.6112	0.4414	5.6112	
1.15	5.3779	-1.2319	5.1883	-0.4740	4.8322	-0.5849	4.5203	-0.3274	4.5203	-0.3274	4.5203	-0.3274	4.5203	-0.3274	4.5203	-0.3274	4.5203	-0.3274	4.5203	-0.3274	4.5203	-0.3274	4.5203	-0.3274	4.5203	-0.3274	4.5203	-0.3274	4.5203	-0.3274	4.5203	-0.3274
1.20	4.0411	-1.5838	4.0411	-1.3585	3.9120	-0.9190	3.6074	-0.6927	3.6074	-0.6927	3.6074	-0.6927	3.6074	-0.6927	3.6074	-0.6927	3.6074	-0.6927	3.6074	-0.6927	3.6074	-0.6927	3.6074	-0.6927	3.6074	-0.6927	3.6074	-0.6927	3.6074	-0.6927		
1.25	3.0663	-1.4420	3.0663	-1.2781	3.1097	-1.2781	3.1599	-0.9366	3.1599	-0.9366	3.1599	-0.9366	3.1599	-0.9366	3.1599	-0.9366	3.1599	-0.9366	3.1599	-0.9366	3.1599	-0.9366	3.1599	-0.9366	3.1599	-0.9366	3.1599	-0.9366	3.1599	-0.9366		
1.30	2.4031	-1.1269	2.4031	-1.0124	2.4775	-1.0124	2.5967	-0.6842	2.5967	-0.6842	2.5967	-0.6842	2.5967	-0.6842	2.5967	-0.6842	2.5967	-0.6842	2.5967	-0.6842	2.5967	-0.6842	2.5967	-0.6842	2.5967	-0.6842	2.5967	-0.6842	2.5967	-0.6842		
1.35	1.9519	-0.7638	2.0401	-0.7638	1.7368	-0.3397	2.0401	-0.6842	2.0401	-0.6842	2.0401	-0.6842	2.0401	-0.6842	2.0401	-0.6842	2.0401	-0.6842	2.0401	-0.6842	2.0401	-0.6842	2.0401	-0.6842	2.0401	-0.6842	2.0401	-0.6842	2.0401	-0.6842		
1.40	1.6408	-0.3945	2.0527	-0.3945	1.7368	-0.3945	2.0527	-0.3945	2.0527	-0.3945	2.0527	-0.3945	2.0527	-0.3945	2.0527	-0.3945	2.0527	-0.3945	2.0527	-0.3945	2.0527	-0.3945	2.0527	-0.3945	2.0527	-0.3945	2.0527	-0.3945	2.0527	-0.3945		
1.45	1.4256	-0.0298	3.4504	-0.0298	2.7748	-0.2379	3.4504	-0.0298	3.4504	-0.0298	3.4504	-0.0298	3.4504	-0.0298	3.4504	-0.0298	3.4504	-0.0298	3.4504	-0.0298	3.4504	-0.0298	3.4504	-0.0298	3.4504	-0.0298	3.4504	-0.0298	3.4504	-0.0298		
1.50	1.2804	0.3306	3.4613	0.3306</																												

## Normalized Admittance Y/Δ of Loop Antennas in Dissipative Media

$\beta\delta$	$\Omega = 11$		$\Omega = 11$		$\Omega = 11$	
	$\frac{\alpha}{\beta} = 0.10$	$\frac{\alpha}{\beta} = 0.30$	$\frac{\alpha}{\beta} = 0.50$	$\frac{\alpha}{\beta} = 0.70$	$\frac{\alpha}{\beta} = 1.00$	
$Y/\Delta$						
0.05	0.02290	-14.0315	0.0865	-14.0432	0.1438	-14.0565
0.10	0.0590	-6.8017	0.1745	-6.8259	0.2894	-6.8757
0.15	0.0904	-4.2945	0.2654	-4.3327	0.4383	-4.4074
0.20	0.1241	-2.9653	0.3607	-3.0200	0.5921	-3.1250
0.25	0.1607	-2.1045	0.4617	-2.1788	0.7522	-2.193
0.30	0.2014	-1.4744	0.5705	-1.5730	0.9201	-1.5555
0.35	0.2476	-0.9724	0.6890	-1.1020	1.0967	-1.3348
0.40	0.3013	-0.5462	0.8196	-0.7159	1.2826	-1.092
0.45	0.3650	-0.1662	0.9649	-0.3985	1.4776	-0.7539
0.50	0.4425	0.1864	1.1277	-0.1055	1.6805	-0.5559
0.55	0.5389	0.5241	1.3106	0.1397	1.8884	-0.4081
0.60	0.5615	0.8552	1.5155	0.3484	2.0972	-0.1065
0.65	0.8204	1.1846	1.7427	0.5178	2.5008	-0.2482
0.70	1.0301	1.5127	1.9896	0.6419	2.4922	-0.2293
0.75	1.3096	1.9324	2.2492	0.7133	2.6643	-0.2441
0.80	1.6821	2.1242	2.5088	0.7257	2.8112	-0.2850
0.85	2.1681	2.3451	2.7508	0.6777	2.9297	-0.3428
0.90	2.7666	2.4230	2.9555	0.5761	3.0194	-0.4080
0.95	3.4193	2.2667	3.1066	0.4372	3.0832	-0.4720
1.00	3.9829	1.8251	3.1964	0.2838	3.1260	-0.5287
1.05	4.2903	1.1739	3.2265	0.1389	3.1537	-0.5744
1.10	4.2368	0.5116	3.2155	0.0202	3.1722	-0.6077
1.15	3.9389	0.0172	3.1740	-0.0631	3.1863	-0.6293
1.20	3.5375	-0.2519	3.1201	-0.1096	3.1999	-0.6408
1.25	3.1447	-0.5308	3.0667	-0.1233	3.2154	-0.6446
1.30	2.8124	-0.2801	3.0223	-0.1110	3.2342	-0.6430
1.35	2.5540	-0.1504	2.9919	-0.0801	3.2567	-0.6583
1.40	2.3661	0.0241	2.9775	-0.0376	3.2830	-0.6521
1.45	2.2412	0.2224	2.9792	0.0106	3.3125	-0.6261
1.50	2.1716	0.4317	2.9959	0.0595	3.3445	-0.6211
1.55	2.1519	0.6436	3.0255	0.1053	3.3780	-0.6178
1.60	2.1787	0.8512	3.0654	0.1450	3.4124	-0.6164
1.65	2.2498	1.0481	3.1128	0.1767	3.4469	-0.6170
1.70	2.3637	1.2265	3.1647	0.1994	3.4809	-0.6194
1.75	2.5180	1.3770	3.2182	0.2130	3.5139	-0.6233
1.80	2.7078	1.4881	3.2707	0.2179	3.5458	-0.6283
1.85	2.9231	1.5474	3.3199	0.2155	3.5764	-0.6342
1.90	3.1478	1.5648	3.3644	0.2307	3.6056	-0.6405
1.95	3.3593	1.4761	3.4031	0.1957	3.6336	-0.6470
2.00	3.5325	1.3480	3.4359	0.1822	3.6604	-0.6535
2.05	3.6463	1.1791	3.4631	0.1687	3.6843	-0.6598
2.10	3.6902	0.9967	3.4856	0.1567	3.7115	-0.6660
2.15	3.6681	0.8288	3.5044	0.1470	3.7360	-0.6718
2.20	3.5949	0.6970	3.5207	0.1403	3.7599	-0.6775
2.25	3.4912	0.6124	3.5357	0.1367	3.7835	-0.6823
2.30	3.3766	0.5765	3.5504	0.1360	3.8068	-0.6882
2.35	3.2669	0.5843	3.5658	0.1377	3.8298	-0.6935
2.40	3.1729	0.6277	3.5822	0.1411	3.8526	-0.6987
2.45	3.1013	0.6975	3.6001	0.1457	3.8751	-0.7039
2.50	3.0555	0.7850	3.6196	0.1508	3.8973	-0.7092

TABLE III  
 Normalized Admittance  $Y/\Delta$  of Loop Antennas in Dissipative Media

$\beta$	$\frac{\alpha}{\beta} = 0.00$	$\frac{\alpha}{\beta} = 0.00$	$\frac{\alpha}{\beta} = 0.00$	$\frac{\alpha}{\beta} = 0.03$	$\frac{\alpha}{\beta} = 0.05$	$\frac{\alpha}{\beta} = 0.07$
	$Y/\Delta$	$Y/\Delta$	$Y/\Delta$	$Y/\Delta$	$Y/\Delta$	$Y/\Delta$
0.05	0.0002 -12.3838	0.0026 -12.3839	0.0075 -12.3840	0.0124 -12.3842	0.0173 -12.3845	0.0224 -12.3848
0.10	0.0008 -6.0079	0.0057 -6.0079	0.0156 -6.0082	0.0254 -6.0086	0.0353 -6.0093	0.0543 -6.0093
0.15	0.0019 -3.7985	0.0094 -3.7986	0.0244 -3.7991	0.0393 -3.7998	0.0543 -3.8009	0.0748 -2.6317
0.20	0.0036 -2.6282	0.0137 -2.6284	0.0341 -2.6291	0.0545 -2.6302	0.0748 -2.6317	0.0973 -1.8754
0.25	0.0060 -1.8703	0.0191 -1.8706	0.0452 -1.8716	0.0713 -1.8732	0.0973 -1.8754	
0.30	0.0095 -1.3150	0.0258 -1.3154	0.0581 -1.3169	0.0905 -1.3192	0.1227 -1.3222	
0.35	0.0146 -0.8711	0.0343 -0.8717	0.0736 -0.8739	0.1128 -0.8771	0.1519 -0.8813	
0.40	0.0213 -0.4917	0.0455 -0.4929	0.0926 -0.4960	0.1596 -0.5005	0.1864 -0.5063	
0.45	0.0323 -0.1495	0.0605 -0.1511	0.1167 -0.1558	0.1726 -0.1622	0.2281 -0.1704	
0.50	0.0474 0.1742	0.0811 0.1716	0.1479 0.1646	0.2142 0.1554	0.2799 0.1438	
0.55	0.0698 0.1934	0.1100 0.4893	0.1896 0.4788	0.2683 0.4652	0.3459 0.4486	
0.60	0.1033 0.8207	0.1516 0.8142	0.2470 0.7950	0.3407 0.7777	0.4324 0.7534	
0.65	0.1544 1.1592	0.2131 1.1587	0.3283 1.1332	0.4403 1.1020	0.5489 1.0657	
0.70	0.2347 1.5533	0.3065 1.5363	0.4470 1.4951	0.5814 1.4463	0.7096 1.3909	
0.75	0.3646 1.9931	0.4544 1.9634	0.6262 1.8945	0.7871 1.8161	0.9369 1.7297	
0.80	0.5833 2.5099	0.6961 2.4564	0.9060 2.3385	1.0952 2.0949	1.2640 2.0727	
0.85	0.9693 3.1257	1.1088 3.0265	1.3561 2.8175	1.5639 2.6016	1.7363 2.3854	
0.90	1.6821 3.5294	1.8378 3.6393	2.0877 3.2657	2.2692 2.9111	2.3977 2.5925	
0.95	3.0140 4.4372	3.1124 4.0862	3.2198 3.4637	3.2489 2.9404	3.2328 2.5022	
1.00	5.1747 4.1923	4.9896 3.7064	4.6349 2.9477	4.3203 2.3843	4.0503 1.9646	
1.05	6.9797 1.9691	6.4182 1.7662	5.5604 1.4470	4.9408 1.2056	4.4768 1.0151	
1.10	6.3872 -0.7830	5.9627 -0.5402	5.2650 -0.2246	4.7283 -0.6478	4.3118 0.6497	
1.15	4.6530 -1.9270	4.5259 -1.6197	4.2584 -1.1427	3.9992 -0.8072	3.7666 -0.5726	
1.20	3.2716 -1.9702	3.2919 -1.7477	3.2807 -1.3532	3.2274 -1.0562	3.1547 -0.8170	
1.25	2.3829 -1.6551	2.4583 -1.5289	2.5554 -1.2596	2.6099 -1.0065	2.6355 -0.8115	
1.30	1.8314 -1.2655	1.9157 -1.1693	2.0552 -0.9858	2.1616 -0.8194	2.2416 -0.6740	
1.35	1.4688 -0.8811	1.5575 -0.8168	1.7149 -0.6922	1.8473 -0.5770	1.9579 -0.4744	
1.40	1.2260 -0.5180	1.3179 -0.4750	1.4842 -0.3920	1.6321 -0.3156	1.7618 -0.2482	
1.45	1.0616 -0.1741	1.1555 -0.1464	1.3314 -0.0948	1.4409 -0.0495	1.6344 -0.0119	
1.50	0.9530 0.1578	1.0514 0.1730	1.2373 0.1983	1.4079 0.2164	1.5630 0.2270	
1.55	0.8886 0.4859	0.9936 0.4894	1.1921 0.4896	1.3745 0.4812	1.5403 0.4650	
1.60	0.8642 0.8179	0.9780 0.8090	1.1922 0.7821	1.3873 0.7450	1.5630 0.6997	
1.65	0.8814 1.1624	1.0067 1.1381	1.2395 1.0783	1.4476 1.0071	1.6315 0.9283	
1.70	0.9487 1.5270	1.0880 1.4918	1.3411 1.3796	1.5605 1.2645	1.7485 1.1455	
1.75	1.0832 1.9184	1.2381 1.8427	1.5097 1.6793	1.7343 1.5096	1.9179 1.3419	
1.80	1.3152 2.3383	1.4838 2.2166	1.7638 1.9683	1.9788 1.7271	2.1428 1.5205	
1.85	1.6044 2.7739	1.8656 2.5923	2.1251 2.2172	2.3613 1.8899	2.4208 1.6049	
1.90	2.2933 3.1723	2.4329 2.9810	2.6079 2.3718	2.6959 1.9569	2.7374 1.6218	
1.95	3.1836 3.3899	3.2132 2.9853	3.1923 2.3471	3.1289 1.8794	3.0591 1.5283	
2.00	4.3153 3.1453	4.1192 2.6969	3.7835 2.0555	3.5260 1.6252	3.3335 1.3182	
2.05	5.2921 2.1830	4.8422 1.8938	4.2051 1.4992	3.7880 1.2175	3.5046 1.0191	
2.10	5.5121 0.7726	5.0070 0.8014	4.3002 0.7920	3.8443 0.7482	3.5399 0.6908	
2.15	4.9312 0.3661	4.5938 -0.1131	4.0706 0.1875	3.7043 0.3340	3.4480 0.3999	
2.20	4.0586 -0.9108	3.9217 -0.6096	3.6575 -0.1953	3.4383 0.0500	3.2701 0.1915	
2.25	3.2688 -1.0093	3.2661 -0.7494	3.2090 -0.3536	3.1297 -0.0900	3.0553 0.0786	
2.30	2.6622 -0.8742	2.7322 -0.6745	2.8088 -0.3473	2.8363 -0.1105	2.8422 0.0514	
2.35	2.2212 -0.6356	2.3283 -0.4892	2.4846 -0.2378	2.5863 -0.0458	2.6541 0.0908	
2.40	1.9063 -0.3555	2.0530 -0.2514	2.2373 -0.0685	2.3889 0.0746	2.5021 0.1774	
2.45	1.6846 -0.0599	1.8233 0.0107	2.0584 0.1342	2.2442 0.2295	2.3899 0.2952	
2.50	1.5338 0.2419	1.6816 0.2847	1.9391 0.3555	2.1489 0.4047	2.3176 0.4320	

Normalized Admittance Y/ $\Delta$  of Loop Antennas in Dissipative Media

 $\Omega = 12$ 

$\frac{\alpha}{\beta}$	$\frac{\alpha}{\beta} = 0.10$		$\frac{\alpha}{\beta} = 0.30$		$\frac{\alpha}{\beta} = 0.50$		$\frac{\alpha}{\beta} = 0.70$		$\frac{\alpha}{\beta} = 1.00$	
	Y/ $\Delta$	Y/ $\Delta$								
0.05	0.0246	-12.3851	0.0734	-12.3951	0.1221	-12.4148	0.1797	-12.4443	0.2433	-12.5069
0.10	0.0500	-6.0107	0.1482	-6.0312	0.2458	-6.0718	0.3426	-6.1323	0.4857	-6.2596
0.15	0.0767	-3.8031	0.2256	-3.8356	0.3725	-3.8991	0.5168	-3.9930	0.7265	-4.1891
0.20	0.1053	-2.6349	0.3066	-2.6814	0.5035	-2.7739	0.6940	-2.9021	1.074	-3.1724
0.25	0.1364	-1.8799	0.3929	-1.9431	0.6403	-2.0632	0.8749	-2.2365	1.973	-2.5867
0.30	0.1710	-1.3283	0.4860	-1.4125	0.7840	-1.5689	1.0591	-1.7901	1.4220	-2.2256
0.35	0.2193	-0.8895	0.5877	-1.0055	0.9356	-1.2067	1.2458	-1.4763	1.6350	-2.0503
0.40	0.2561	-0.5175	0.7003	-0.6632	1.0958	-0.9165	1.4331	-1.2528	1.8323	-1.8652
0.45	0.3105	-0.1958	0.8262	-0.3774	1.2644	-0.6944	1.6182	-1.0966	2.0105	-1.7931
0.50	0.3770	-0.1224	0.9680	-0.1304	1.4405	-0.5232	1.7973	-0.9940	2.1670	-1.7552
0.55	0.4599	0.4184	1.1283	0.0835	1.6215	-0.3969	1.9661	-0.9351	2.3608	-1.7675
0.60	0.5660	0.7100	1.3092	0.2652	1.8035	-0.3123	2.1203	-0.9117	2.4126	-1.7890
0.65	0.7047	1.0025	1.5114	0.4119	1.9810	-0.2670	2.2562	-0.9161	2.5643	-1.8214
0.70	0.8897	1.2971	1.7328	0.5174	2.1471	-0.2578	2.3715	-0.9402	2.5789	-1.8585
0.75	1.1403	1.5888	1.9670	0.5739	2.2951	-0.2796	2.4657	-0.9767	2.6398	-1.8962
0.80	1.4814	1.8602	2.0201	0.5746	2.5721	-0.3251	2.5450	-1.0167	2.6903	-1.9323
0.85	1.9387	2.0703	2.4203	0.5172	2.5159	-0.3855	2.5972	-1.0612	2.7332	-1.9653
0.90	2.5192	2.1430	2.6016	0.4083	2.8556	-0.4514	2.6408	-1.004	2.7079	-1.9753
0.95	3.1671	1.9724	2.7293	0.2644	2.6309	-0.5149	2.6744	-1.343	2.8051	-2.0225
1.00	3.7210	1.4915	2.7960	0.1090	2.6570	-0.5700	2.7015	-1.1622	2.8369	-2.0471
1.05	3.9720	0.7912	2.8065	-0.0341	2.6699	-0.6135	2.7248	-1.1845	2.8671	-2.0699
1.10	3.8479	0.1131	2.7747	-0.1480	2.6752	-0.6445	2.7463	-1.2019	2.8961	-2.0913
1.15	3.4768	-0.3481	2.7184	-0.2245	2.6776	-0.6640	2.7673	-1.2155	2.9242	-2.1117
1.20	3.0383	-0.5602	2.6557	-0.2641	2.6806	-0.6740	2.7887	-1.2264	2.9514	-2.1313
1.25	2.6421	-0.5859	2.5928	-0.2721	2.6864	-0.6768	2.8107	-1.2356	2.9779	-2.1505
1.30	2.3258	-0.4980	2.5435	-0.2559	2.6960	-0.6749	2.8334	-1.2439	3.0035	-2.1693
1.35	2.0906	-0.3481	2.5095	-0.2232	2.7098	-0.6703	2.8567	-1.2519	3.0263	-2.1878
1.40	1.9261	-0.1669	2.4921	-0.1809	2.7275	-0.6649	2.8803	-1.2600	3.0523	-2.2060
1.45	1.8213	0.0286	2.4909	-0.1347	2.7484	-0.6599	2.9039	-1.2684	3.0755	-2.2241
1.50	1.7673	0.2287	2.5043	-0.0892	2.7717	-0.6563	2.9273	-1.2772	3.0979	-2.2419
1.55	1.7583	0.4277	2.5300	-0.0479	2.7966	-0.6545	2.9503	-1.2865	3.1193	-2.2595
1.60	1.7913	0.6207	2.5653	-0.0153	2.8222	-0.6548	2.9728	-1.2961	3.1403	-2.2769
1.65	1.8649	0.8028	2.6074	0.0123	2.8477	-0.6570	2.9946	-1.3061	3.1604	-2.2941
1.70	1.9786	0.9673	2.6532	0.0297	2.8728	-0.6610	3.0157	-1.3162	3.1798	-2.3110
1.75	2.1314	1.1049	2.6999	0.0375	2.8968	-0.6665	3.0361	-1.3265	3.1986	-2.3277
1.80	2.3197	1.2040	2.7450	0.0369	2.9197	-0.6729	3.0659	-1.3368	3.2167	-2.3442
1.85	2.5346	1.2506	2.7862	0.0291	2.9413	-0.6800	3.0749	-1.3472	3.2343	-2.3604
1.90	2.7594	1.2325	2.8223	0.0160	2.9616	-0.6875	3.0934	-1.3574	3.2513	-2.3765
1.95	2.9691	1.1438	2.8522	-0.0302	2.9808	-0.6950	3.1113	-1.3676	3.2677	-2.3923
2.00	3.1349	0.9918	2.8760	-0.0175	2.9990	-0.7024	3.1287	-1.3778	3.2836	-2.4079
2.05	3.2323	0.7986	2.8943	-0.0343	3.0163	-0.7095	3.1457	-1.3878	3.2996	-2.4234
2.10	3.2512	0.5972	2.9079	-0.0490	3.0330	-0.7164	3.1622	-1.3977	3.3139	-2.4386
2.15	3.1994	0.4199	2.9181	-0.0608	3.0492	-0.7229	3.1783	-1.4076	3.3284	-2.4537
2.20	3.0976	0.2890	2.9263	-0.0692	3.0651	-0.7291	3.1940	-1.4174	3.3424	-2.4686
2.25	2.9705	0.2132	2.9336	-0.0743	3.0807	-0.7352	3.2094	-1.4272	3.3560	-2.4833
2.30	2.8395	0.1900	2.9410	-0.0765	3.0961	-0.7410	3.2244	-1.4369	3.3692	-2.4979
2.35	2.7212	0.2109	2.9491	-0.0762	3.1113	-0.7468	3.2390	-1.4465	3.3820	-2.5123
2.40	2.6238	0.2655	2.9594	-0.0742	3.1264	-0.7525	3.2534	-1.4561	3.3944	-2.5265
2.45	2.5523	0.3436	2.9711	-0.0712	3.1413	-0.7583	3.2674	-1.4657	3.4064	-2.5406
2.50	2.5088	0.4362	2.9845	-0.0679	3.1561	-0.7641	3.2811	-1.4781	3.4180	-2.5545

TABLE IV  
Normalized Admittance  $Y/\Delta$  of Loop Antennas in Dissipative Media

$\beta$	$\Omega = 15$			$\Omega = 15$		
	$\frac{\alpha}{\beta} = 0.06$	$\frac{\alpha}{\beta} = 0.01$	$\frac{\alpha}{\beta} = 0.03$	$\frac{\alpha}{\beta} = 0.05$	$\frac{\alpha}{\beta} = 0.07$	$\frac{\alpha}{\beta} = 0.09$
0.05	0.0001 -9.1554	0.0018 -9.1554	0.0052 -9.1555	0.0086 -9.1556	0.0119 -9.1558	0.0149 -9.1558
0.10	0.0004 -4.4503	0.0038 -4.4503	0.0107 -4.4505	0.0175 -4.4508	0.0243 -4.4512	0.0374 -4.4512
0.15	0.0010 -2.8236	0.0062 -2.8236	0.0166 -2.8239	0.0270 -2.8244	0.0374 -2.8251	0.0474 -2.8251
0.20	0.0019 -1.9645	0.0090 -1.9646	0.0232 -1.9651	0.0373 -1.9658	0.0514 -1.9669	0.0669 -1.9669
0.25	0.0033 -1.4101	0.0124 -1.4103	0.0306 -1.4109	0.0487 -1.4120	0.0669 -1.4135	0.0842 -1.4135
0.30	0.0052 -1.0053	0.0165 -1.0056	0.0391 -1.0065	0.0617 -1.0080	0.0842 -1.0101	0.1042 -1.0101
0.35	0.0080 -0.6827	0.0218 -0.6831	0.0493 -0.6845	0.0768 -0.6966	0.1042 -0.6894	0.1278 -0.4171
0.40	0.0120 -0.4077	0.0286 -0.4083	0.0618 -0.4103	0.0949 -0.4132	0.1278 -0.1732	0.1918 -0.0556
0.45	0.0178 -0.1597	0.0377 -0.1606	0.0775 -0.1635	0.1170 -0.1677	0.1563 -0.1732	0.1918 -0.0556
0.50	0.0262 -0.0751	0.0501 -0.0736	0.0977 -0.0693	0.1450 -0.0633	0.1918 -0.0556	0.1918 -0.0556
0.55	0.0386 0.3076	0.0674 0.3052	0.1247 0.2987	0.1814 0.2899	0.2373 0.2787	0.2972 0.5041
0.60	0.0574 0.5477	0.0925 0.5439	0.1619 0.5339	0.2502 0.5206	0.3789 0.7388	0.4938 0.9891
0.65	0.0865 0.8065	0.1298 0.8003	0.2150 0.7843	0.2981 0.7637	0.4360 0.6579	0.5614 1.2594
0.70	0.1330 1.0977	0.1874 1.0872	0.2937 1.0609	0.3960 1.0280	0.5429 0.9137	0.6614 1.5476
0.75	0.2105 1.4408	0.2807 1.4221	0.4158 1.3769	0.5729 1.6523	0.7708 1.3024	0.9316 1.8316
0.80	0.3471 1.8645	0.4403 1.8295	0.6149 1.7474	0.7748 1.7178	0.9708 2.3338	1.0960 2.0330
0.85	0.6069 2.4125	0.7334 2.3416	0.9588 2.1930	1.1478 2.0103	1.3469 1.7177	1.5390 1.3264
0.90	1.1506 3.1369	1.3176 2.9793	1.5834 2.6539	1.7708 2.3338	1.9669 2.0330	2.1469 1.9565
0.95	2.4073 3.9786	2.5577 3.6081	2.7152 2.9469	2.7497 2.4001	2.7777 2.1777	2.8015 1.7177
1.00	5.1475 3.9093	4.8714 3.2605	4.3462 2.3426	3.9015 1.7177	3.5390 1.3264	3.9015 1.3264
1.05	7.1521 0.2902	6.3132 0.3242	5.1358 0.3176	4.3563 0.2758	3.8075 0.2255	3.5777 0.6988
1.10	4.8807 -2.5090	4.6364 -2.0294	4.1444 -1.3637	3.7130 -0.9550	3.3577 -0.6579	3.0777 -1.0977
1.15	2.8139 -2.5757	2.8608 -2.2910	2.8541 -1.7777	2.7712 -1.3890	2.6579 -1.0621	2.5746 -1.1262
1.20	1.7662 -2.0714	1.8597 -1.9144	1.9844 -1.6150	2.0448 -1.3498	2.0621 -1.3498	2.0621 -1.1262
1.25	1.2225 -1.5815	1.3131 -1.4928	1.4598 -1.3141	1.5655 -1.1434	1.6381 -0.9688	1.6381 -0.9688
1.30	0.9134 -1.1718	0.9954 -1.1182	1.1394 -1.0073	1.2576 -0.8973	1.3524 -0.7937	1.4576 -0.7937
1.35	0.7239 -0.8280	0.7994 -0.7940	0.9380 -0.7234	1.0592 -0.6526	1.1638 -0.5850	1.2638 -0.5850
1.40	0.6016 -0.5295	0.6738 -0.5077	0.8094 -0.4632	0.9325 -0.4194	1.0427 -0.3783	1.1463 -0.3783
1.45	0.5214 -0.2599	0.5920 -0.2466	0.7293 -0.2210	0.8555 -0.1977	0.9707 -0.1777	1.0777 -0.1777
1.50	0.4702 -0.0366	0.5439 -0.0001	0.6848 0.0099	0.8163 0.0156	0.9372 0.0169	0.9372 0.0169
1.55	0.4422 0.2409	0.5203 0.2409	0.6699 0.2358	0.8092 0.2241	0.9371 0.2067	0.9690 0.3927
1.60	0.4354 0.4918	0.5209 0.4946	0.6835 0.4623	0.8332 0.4310	0.9410 0.3448	0.9648 0.5747
1.65	0.4520 0.7555	0.5481 0.7390	0.7283 0.6947	0.8909 0.6387	0.9690 0.5387	1.0346 0.7503
1.70	0.4988 1.0429	0.6095 1.0125	0.8123 0.9369	0.9889 0.8473	1.0351 1.1394	1.1268 0.7503
1.75	0.5901 1.3663	0.7201 1.3135	0.9497 1.1905	1.1384 1.0532	1.2448 1.2898	1.3456 0.9126
1.80	0.7540 1.7408	0.9083 1.6506	1.1639 1.4509	1.3551 1.2448	1.4937 1.4937	1.6479 1.0479
1.85	1.0470 2.1790	1.2257 2.0204	1.4899 1.6972	1.6560 1.3957	1.7552 1.7552	1.8188 1.1318
1.90	1.5822 2.6677	1.7624 2.3840	1.9692 1.8714	2.0488 2.0488	2.0643 2.0643	2.0643 1.1287
1.95	2.5642 3.0700	2.6377 2.5848	2.6124 1.8484	2.5029 1.3478	2.8333 1.0005	2.6400 0.7342
2.00	4.1394 2.8425	3.8244 2.2215	3.2960 1.4524	2.9132 1.0125	2.6400 0.7342	2.6400 0.7342
2.05	5.4573 1.1474	4.6704 0.9285	3.6910 0.6556	3.1192 0.4895	2.7553 0.3745	2.6983 0.0167
2.10	4.9449 -0.9671	4.3613 -0.5862	3.5472 -0.2063	3.0348 -0.0492	2.6500 -0.2522	2.5100 -0.3999
2.15	3.5420 -1.8088	3.3844 -1.3482	3.0341 -0.7565	2.7364 -0.4326	2.2650 -0.6141	2.2650 -0.6141
2.20	2.4554 -1.7836	2.5010 -1.4552	2.4674 -0.9489	2.3691 -0.6141	2.0317 -0.6384	2.0317 -0.4406
2.25	1.7788 -1.4964	1.8886 -1.2847	2.0019 -0.9178	2.0019 -0.6160	1.7602 -0.5666	1.8160 -0.4052
2.30	1.3627 -1.1686	1.4859 -1.0324	1.6593 -0.7778	1.4176 -0.5948	1.5564 -0.4432	1.6527 -0.3222
2.35	1.0987 -0.8571	1.2218 -0.7680	1.4175 -0.5948	1.4175 -0.3969	1.4112 -0.2944	1.5330 -0.2116
2.40	0.9260 -0.5702	1.0466 -0.5119	1.2515 -0.3969	1.4117 -0.1956	1.3145 -0.1340	1.4528 -0.0861
2.45	0.8119 -0.3036	0.9312 -0.2667	1.1417 -0.1956	1.0759 -0.0553	1.2585 -0.0311	1.4081 -0.0461
2.50	0.7387 -0.0499	0.8592 -0.0298	1.0759 -0.0053	1.0759 -0.0053	1.0759 -0.0053	1.0759 -0.0053

Normalized Admittance  $Y/\Delta$  of Loop Antennas in Dissipative Media

 $\Omega = 15$ 

$\beta$	$\frac{\alpha}{\beta} = 0.10$	$\frac{\alpha}{\beta} = 0.30$	$\frac{\alpha}{\beta} = 0.50$	$\frac{\alpha}{\beta} = 0.70$	$\frac{\alpha}{\beta} = 1.00$	
0.05	0.0170	-9.1563	0.0508	-9.1632	0.0845	-9.1768
0.10	0.0346	-4.4522	0.1026	-4.4664	0.1702	-4.4945
0.15	0.0529	-2.8266	0.1562	-2.8491	0.2581	-2.9932
0.20	0.0726	-1.9690	0.2126	-2.0112	0.3494	-2.0635
0.25	0.0940	-1.4165	0.2728	-1.4604	0.4449	-1.5443
0.30	0.1179	-1.6142	0.3380	-1.0728	0.5458	-1.1828
0.35	0.1451	-0.6950	0.4098	-0.7726	0.6529	-0.9143
0.40	0.1769	-0.4248	0.4898	-0.5273	0.7669	-0.9477
0.45	0.2145	-0.1837	0.5801	-0.3194	0.8276	-0.5475
0.50	0.2612	0.0409	0.6829	-0.1398	1.0146	-0.4252
0.55	0.3195	0.2579	0.8006	0.0158	1.1460	-0.3370
0.60	0.3949	0.4740	0.9352	0.1478	1.2785	-0.2811
0.65	0.4949	0.6941	1.0580	0.2532	1.4076	-0.6256
0.70	0.6314	0.9212	1.2580	0.3263	1.5273	-0.2596
0.75	0.8221	1.1537	1.4403	0.3592	1.6316	-0.2079
0.80	1.0933	1.3800	1.6242	0.3444	1.7154	-0.3347
0.85	1.4784	1.5656	1.7931	0.2788	1.7758	-0.3920
0.90	2.0097	1.6315	1.9274	0.1682	1.8133	-0.4517
0.95	2.6147	1.4445	2.0105	0.0294	1.8308	-0.5068
1.00	3.1199	0.9046	2.0375	-0.1139	1.8335	-0.5526
1.05	3.2415	0.1506	2.0148	-0.2388	1.8268	-0.5869
1.10	2.9489	-0.4763	1.9589	-0.3309	1.8159	-0.6297
1.15	2.4815	-0.7973	1.8878	-0.3859	1.8046	-0.6224
1.20	2.0429	-0.8667	1.8163	-0.4074	1.7956	-0.6273
1.25	1.7024	-0.7948	1.7540	-0.4324	1.7904	-0.6267
1.30	1.4598	-0.6578	1.7059	-0.3792	1.7894	-0.6228
1.35	1.2923	-0.4951	1.6737	-0.3447	1.7926	-0.6175
1.40	1.1848	-0.3251	1.6572	-0.3050	1.7995	-0.6123
1.45	1.1229	-0.1554	1.6550	-0.2645	1.8092	-0.6080
1.50	1.0983	0.0107	1.6651	-0.2268	1.8210	-0.6054
1.55	1.1065	0.1716	1.6852	-0.1944	1.8340	-0.6047
1.60	1.1458	0.3258	1.7129	-0.1692	1.8473	-0.6059
1.65	1.2166	0.4707	1.7453	-0.1522	1.8605	-0.6089
1.70	1.3203	0.6016	1.7800	-0.1439	1.9731	-0.6134
1.75	1.4586	0.7104	1.8143	-0.1439	1.8347	-0.6190
1.80	1.6306	0.7951	1.8459	-0.1513	1.8952	-0.6254
1.85	1.8298	0.8097	1.8731	-0.1645	1.9046	-0.6321
1.90	2.0394	0.7681	1.8948	-0.1817	1.9130	-0.6389
1.95	2.2303	0.6512	1.9104	-0.2007	1.9204	-0.6456
2.00	2.3663	0.4680	1.9203	-0.2197	1.9272	-0.6520
2.05	2.4187	0.2503	1.9253	-0.2371	1.9333	-0.6580
2.10	2.3625	0.0418	1.9265	-0.2516	1.9391	-0.6637
2.15	2.2778	-0.1205	1.9252	-0.2627	1.9447	-0.6690
2.20	2.1369	-0.2198	1.9228	-0.2703	1.9501	-0.6740
2.25	1.9897	-0.2578	1.9204	-0.2746	1.9555	-0.6787
2.30	1.8558	-0.2461	1.9189	-0.2762	1.9609	-0.6833
2.35	1.7454	-0.1988	1.9189	-0.2756	1.9663	-0.6879
2.40	1.6623	-0.1280	1.9209	-0.2738	1.9716	-0.6924
2.45	1.6070	-0.0433	1.9247	-0.2714	1.9770	-0.6959
2.50	1.5782	0.0482	1.9304	-0.2691	1.9823	-0.7015

TABLE V  
Normalized Admittance  $Y/\Delta$  of Loop Antennas in Dissipative Media  
 $\Omega = 1.7$

$\beta b$	$\frac{a}{E} = 6.00$	$\frac{a}{E} = 0.01$	$\frac{a}{E} = 0.03$	$\frac{a}{E} = 0.05$	$\frac{a}{E} = 0.07$
0.05	0.0001 -7.5205	0.0014 -7.5205	0.0041 -7.5206	0.0068 -7.5207	0.0095 -7.5209
0.10	0.0003 -3.6585	0.0030 -3.6586	0.0085 -3.6587	0.0139 -3.6589	0.0194 -3.6593
0.15	0.0007 -2.3246	0.0048 -2.3247	0.0131 -2.3249	0.0214 -2.3253	0.0297 -2.3258
0.20	0.0013 -1.6211	0.0070 -1.6211	0.0183 -1.6215	0.0296 -1.6221	0.0409 -1.6229
0.25	0.0022 -1.1677	0.0095 -1.1678	0.0241 -1.1683	0.0386 -1.1692	0.0531 -1.1703
0.30	0.0035 -0.8372	0.0126 -0.8373	0.0307 -0.8381	0.0488 -0.8392	0.0668 -0.8408
0.35	0.0054 -0.5741	0.0165 -0.5744	0.0386 -0.5754	0.0606 -0.5770	0.0826 -0.5792
0.40	0.0081 -0.3500	0.0215 -0.3504	0.0482 -0.3519	0.0748 -0.3541	0.1013 -0.3572
0.45	0.0120 -0.1479	0.0281 -0.1486	0.0602 -0.1507	0.0921 -0.1539	0.1238 -0.1582
0.50	0.0177 0.0435	0.0371 0.0424	0.0756 0.0393	0.1139 0.0347	0.1518 0.0287
0.55	0.0262 0.2333	0.0496 0.2317	0.0952 0.2269	0.1422 0.2201	0.1877 0.2115
0.60	0.0391 0.4302	0.0677 0.4275	0.1245 0.4201	0.1804 0.4099	0.2352 0.3971
0.65	0.0591 0.6436	0.0947 0.6392	0.1649 0.6273	0.2336 0.6115	0.3003 0.5919
0.70	0.0913 0.8859	0.1366 0.8784	0.2253 0.8588	0.3108 0.8332	0.3928 0.8023
0.75	0.1459 1.1755	0.2053 1.1621	0.3200 1.1277	0.4284 1.0845	0.5296 1.0338
0.80	0.2444 1.5418	0.3254 1.5153	0.4781 1.4781	0.6167 1.3748	0.7405 1.2878
0.85	0.4389 2.0347	0.5542 1.9795	0.7611 1.8503	0.9351 1.7039	1.1490 1.5490
0.90	0.8742 2.7367	1.0412 2.6034	1.3092 2.3164	1.4950 2.0251	1.6171 1.7480
0.95	2.0206 3.6945	2.2073 3.3272	2.4020 2.6627	2.4446 2.1152	2.4977 1.6792
1.00	5.1373 3.8032	4.7483 3.0269	4.1369 2.0126	3.6118 1.4047	3.2029 1.0128
1.05	6.9020 0.9520	5.9742 -0.6197	4.7075 -0.2997	3.8984 -0.1729	3.3449 -0.1219
1.10	3.6382 -2.9701	3.5838 -2.4677	3.3293 -1.7242	3.0334 -1.2433	2.7606 -0.9319
1.15	1.8759 -2.4507	1.9639 -2.2219	2.0919 -1.7993	2.1619 -1.4479	2.0591 -1.1711
1.20	1.1348 -1.8366	1.2374 -1.7272	1.3914 -1.5038	1.4866 -1.2916	1.5375 -1.1C33
1.25	0.7756 -1.3653	0.8601 -1.3053	1.0036 -1.1893	1.1141 -1.0522	1.1957 -0.9305
1.30	0.5773 -1.0303	0.6487 -0.9682	0.7775 -0.8925	0.8868 -0.8132	0.9773 -0.7352
1.35	0.4575 -0.7109	0.5211 -0.6892	0.6396 -0.6421	0.7455 -0.5927	0.8380 -0.5436
1.40	0.3610 -0.4625	0.4406 -0.4438	0.5539 -0.4200	0.6582 -0.3955	0.7528 -0.3620
1.45	0.3313 -0.2407	0.3899 -0.2326	0.5025 -0.2169	0.6077 -0.2025	0.7047 -0.1920
1.50	0.3002 -0.0334	0.3603 -0.0298	0.4761 -0.0250	0.5850 -0.0236	0.6860 -0.0255
1.55	0.2640 0.1691	0.3479 0.1634	0.4709 0.1623	0.5863 0.1507	0.6929 0.1342
1.60	0.2517 0.3752	0.3521 0.3675	0.4866 0.3509	0.6114 0.3240	0.7250 0.2907
1.65	0.2953 0.5939	0.3753 0.5914	0.5263 0.5460	0.6632 0.4944	0.7948 0.4449
1.70	0.3301 0.8357	0.4239 0.8130	0.5972 0.7528	0.7436 0.6762	0.8776 0.5953
1.75	0.3976 1.1146	0.5111 1.0749	0.7129 0.9750	0.8790 0.8586	1.0112 0.7365
1.80	0.5216 1.4501	0.6624 1.3791	0.8971 1.2119	1.0715 1.0317	1.1952 0.8562
1.85	0.7542 1.8676	0.9297 1.7349	1.1889 1.4489	1.3475 1.1732	1.4365 0.9302
1.90	1.2167 2.3958	1.4178 2.1237	1.6440 1.6321	1.7225 1.2303	1.7285 0.9202
1.95	2.1930 2.9156	2.3105 2.3957	2.4976 1.6184	2.1705 1.1143	2.0322 0.7917
2.00	4.0749 2.7502	3.6688 1.9994	3.0131 1.1685	2.5679 0.7461	2.2652 0.4992
2.05	5.5169 0.3773	4.4957 0.3382	3.3397 0.2537	2.7168 0.1951	2.3382 0.1304
2.10	4.1584 -1.8453	3.7161 -1.2369	3.0115 -0.6120	2.5427 -0.3395	2.2308 -0.2100
2.15	2.5313 -2.1189	2.5417 -1.6614	2.3870 -1.0227	2.1843 -0.6509	2.0C87 -0.4353
2.20	1.6193 -1.7831	1.7409 -1.5201	1.8305 -0.7020	1.8125 -0.4125	1.7580 -0.5324
2.25	1.1521 -1.3992	1.2637 -1.2461	1.4307 -0.9550	1.5070 -0.7146	1.5328 -0.5325
2.30	0.8541 -1.0616	0.9759 -0.9692	1.1608 -0.7809	1.2798 -0.6108	1.3525 -0.4725
2.35	0.6947 -0.7746	0.7960 -0.7164	0.9810 -0.5939	1.1199 -0.4780	1.2181 -0.3796
2.40	0.5766 -0.5244	0.6806 -0.4873	0.9628 -0.4091	1.0996 -0.3342	1.1243 -0.2701
2.45	0.5666 -0.2986	0.6070 -0.2766	0.7881 -0.2299	0.9405 -0.1876	1.0648 -0.1532
2.50	0.4627 -0.0871	0.5630 -0.0756	0.7464 -0.0556	0.9040 -0.0414	0.9351 -0.0341

Normalized Admittance  $\gamma/\Delta$  of Loop Antennas in Dissipative Media

 $\Omega = 17$ 

$\beta\alpha$	$\frac{\alpha}{\beta} = 0.10$			$\frac{\alpha}{\beta} = 0.30$			$\frac{\alpha}{\beta} = 0.50$			$\frac{\alpha}{\beta} = 0.70$		
	$\gamma/\Delta$	$\gamma/\Delta$	$\gamma/\Delta$									
0.05	0.0136	-7.5212	0.0405	-7.5267	0.0675	-7.5376	0.0943	-7.5539	0.1345	-7.5885	0.1990	-7.6266
0.10	0.0275	-3.6600	0.0819	-3.6714	0.1359	-3.6938	0.1894	-3.7272	0.2686	-3.7477	0.4019	-3.7541
0.15	0.0422	-2.3270	0.1247	-2.3449	0.2061	-2.3801	0.2960	-2.4322	0.4019	-2.4322	0.5338	-1.9242
0.20	0.0578	-1.6246	0.1697	-1.6502	0.2791	-1.7001	0.3647	-1.7733	0.4859	-1.8724	0.6629	-1.5691
0.25	0.0749	-1.1727	0.2179	-1.2077	0.3557	-1.2750	0.4859	-1.3724	0.6629	-1.3724	0.7971	-1.3507
0.30	0.0939	-0.8441	0.2703	-0.8909	0.4368	-0.9792	0.5894	-1.1046	0.9041	-1.2153	1.0404	-1.1355
0.35	0.1155	-0.5836	0.3281	-0.6458	0.5232	-0.7599	0.6948	-0.9175	0.8010	-0.7858	0.9111	-1.0403
0.40	0.1408	-0.3632	0.3927	-0.4455	0.6153	-0.5915	0.8010	-0.962	0.6957	-1.057	1.057	-1.0803
0.45	0.1709	-0.1665	0.4666	-0.2758	0.7133	-0.4611	0.962	-0.6393	0.866	-1.057	1.057	-1.0803
0.50	0.2171	0.5498	-0.1291	0.8167	-0.3622	1.0076	-0.6393	1.086	-1.0803	1.086	-1.0803	1.086
0.55	0.2547	0.1950	0.6464	-0.0319	0.9240	-0.2916	1.1022	-0.6106	1.2513	-1.0843	1.3021	-1.0993
0.60	0.3153	0.3732	0.7577	0.1060	1.0325	-0.2481	1.1867	-0.6045	1.399	-1.1197	1.3670	-1.1415
0.65	0.3964	0.5562	0.8850	0.1918	1.1380	-0.2308	1.2585	-0.6159	1.3670	-1.1415	1.3670	-1.1415
0.70	0.5082	0.7474	1.0276	0.2501	1.2354	-0.2300	1.3157	-0.6392	1.3859	-1.1624	1.3859	-1.1624
0.75	0.6670	0.9467	1.1819	0.2736	1.3192	-0.2661	1.3848	-0.6692	1.3990	-1.1810	1.3990	-1.1810
0.80	0.8980	1.1458	1.3378	0.2548	1.3984	-0.3098	1.3671	-0.7009	1.4047	-1.1969	1.4047	-1.1969
0.85	1.2355	1.3150	1.4601	0.1906	1.4297	-0.3618	1.4140	-0.7569	1.4512	-1.2103	1.4209	-1.2216
0.90	1.7134	1.3777	1.5900	0.0862	1.4545	-0.4148	1.4178	-0.7778	1.4260	-1.2512	1.4260	-1.2512
0.95	2.2912	1.1906	1.6524	-0.0421	1.4622	-0.4627	1.4186	-0.7936	1.4260	-1.2512	1.4260	-1.2512
1.00	2.7504	0.6387	1.6628	-0.1712	1.4576	-0.5015	1.4275	-0.8050	1.4308	-1.2496	1.4308	-1.2496
1.05	2.7862	-0.1033	1.6296	-0.2800	1.4458	-0.5296	1.4183	-0.8129	1.4356	-1.2472	1.4418	-1.2543
1.10	2.4265	-0.6519	1.5692	-0.3564	1.4312	-0.5473	1.4172	-0.5562	1.4183	-0.8183	1.4403	-1.2612
1.15	1.9561	-0.8737	1.4987	-0.3982	1.4103	-0.4103	1.4059	-0.5584	1.4206	-0.8220	1.4449	-1.2678
1.20	1.5609	-0.8741	1.4311	-0.4311	1.3741	-0.4005	1.3984	-0.5562	1.4236	-0.8256	1.4494	-1.2743
1.25	1.2759	-0.7706	1.3741	-0.4005	1.3313	-0.3751	1.3951	-0.5515	1.4275	-0.8277	1.4537	-1.2803
1.30	1.0821	-0.6282	1.3282	-0.3419	1.3023	-0.3419	1.3956	-0.5459	1.4323	-0.8305	1.4577	-1.2872
1.35	0.9550	-0.4755	1.2894	-0.3054	1.2894	-0.3054	1.3994	-0.5406	1.4376	-0.8336	1.4615	-1.2935
1.40	0.8763	-0.3237	1.2681	-0.2681	1.2681	-0.2681	1.4057	-0.5365	1.4430	-0.8372	1.4650	-1.2935
1.45	0.8341	-0.1764	1.2973	-0.2366	1.2973	-0.2366	1.4137	-0.5340	1.4484	-0.8412	1.4682	-1.2997
1.50	0.8213	-0.0345	1.2973	-0.2366	1.3150	-0.2092	1.4227	-0.5334	1.4537	-0.8453	1.4812	-1.3059
1.55	0.8347	0.1019	1.3388	-0.1886	1.4319	-0.5345	1.4586	-0.8502	1.4738	-1.3119	1.4762	-1.3179
1.60	0.8733	0.2323	1.3664	-0.1756	1.4049	-0.5372	1.4632	-0.8551	1.4820	-1.3350	1.4820	-1.3350
1.65	0.9381	0.3550	1.4662	0.1705	1.4493	-0.5411	1.4675	-0.8661	1.4974	-1.3405	1.4974	-1.3405
1.70	1.0315	0.4662	1.3954	0.1705	1.4236	-0.1728	1.4567	-0.5460	1.4749	-0.8751	1.4991	-1.3459
1.75	1.1559	0.5586	1.4662	0.1705	1.4662	-0.1728	1.4632	-0.5515	1.4782	-0.8800	1.4812	-1.3512
1.80	1.3119	0.6208	1.4849	-0.1915	1.4687	-0.1915	1.4687	-0.5572	1.4812	-0.8848	1.4861	-1.3512
1.85	1.4943	0.6363	1.4899	-0.1951	1.4855	-0.2119	1.4733	-0.5628	1.4839	-0.8884	1.4861	-1.3512
1.90	1.6870	0.5676	1.4646	0.1956	1.4646	-0.2299	1.4772	-0.5683	1.4865	-0.8894	1.4871	-1.3564
1.95	1.6595	0.4666	1.5005	-0.2474	1.4805	-0.5735	1.4889	-0.8940	1.4879	-1.3615	1.4886	-1.3665
2.00	1.9729	0.2780	1.5005	-0.2474	1.4834	-0.5783	1.4912	-0.8986	1.4986	-1.3665	1.4986	-1.3665
2.05	1.9987	0.0641	1.4985	-0.2754	1.4860	-0.5827	1.4934	-0.9030	1.4991	-1.3715	1.4991	-1.3715
2.10	1.9374	-0.1293	1.4941	-0.2847	1.4885	-0.5868	1.4954	-0.9074	1.4985	-1.3763	1.4985	-1.3763
2.15	1.8164	-0.2673	1.4941	-0.2847	1.4910	-0.5906	1.4973	-0.9118	1.4987	-1.3811	1.4987	-1.3811
2.20	1.6716	-0.3397	1.4890	-0.2906	1.4934	-0.5942	1.4959	-0.9161	1.4986	-1.3858	1.4986	-1.3858
2.25	1.5312	-0.3549	1.4843	-0.2935	1.4807	-0.2940	1.4959	-0.5977	1.5019	-0.9204	1.4988	-1.3924
2.30	1.4106	-0.3277	1.4807	-0.2940	1.4733	-0.6011	1.5025	-0.9247	1.4987	-1.3950	1.4987	-1.3950
2.35	1.3159	-0.2728	1.4788	-0.2928	1.4788	-0.6045	1.5037	-0.6080	1.5040	-0.9289	1.4989	-1.3994
2.40	1.2472	-0.2102	1.4788	-0.2906	1.4788	-0.6045	1.5064	-0.6115	1.5064	-0.9331	1.4981	-1.4039
2.45	1.2051	-0.1207	1.4806	-0.2881	1.4806	-0.6080	1.5064	-0.6115	1.5064	-0.9331	1.4981	-1.4039
2.50	1.1857	-0.0369	1.4841	-0.2856	1.4841	-0.6080	1.5064	-0.6115	1.5064	-0.9331	1.4981	-1.4039

TABLE VI  
Normalized Admittance  $\bar{Y}/\Delta$  of Loop Antennas in Dissipative Media  
 $\Omega = \frac{\omega}{c}$

$\frac{\alpha}{\beta} = 0.00$	$\frac{\alpha}{\beta} = 0.01$	$\frac{\alpha}{\beta} = 0.03$	$\frac{\alpha}{\beta} = 0.05$
$\bar{Y}_{11}$	$\bar{Y}_{12}$	$\bar{Y}_{11}$	$\bar{Y}_{12}$
0.05 0.0301 -6.3809	0.0012 -6.3810	0.0034 -6.3816	0.0057 -6.3811
0.10 0.0322 -3.1057	0.0025 -3.1058	0.0070 -3.1054	0.0116 -3.1061
0.15 0.0605 -1.9752	0.0040 -1.9752	0.0109 -1.9754	0.0178 -1.9757
0.20 0.0094 -1.3724	0.0057 -1.3724	0.0151 -1.3727	0.0245 -1.3802
0.25 0.0016 -0.9958	0.0077 -0.9959	0.0198 -0.9963	0.0319 -0.9970
0.30 0.0326 -0.7164	0.0101 -0.7165	0.0252 -0.7171	0.0403 -0.7180
0.35 0.0339 -0.4942	0.0132 -0.4944	0.0316 -0.4952	0.0501 -0.4965
0.40 0.559 -0.3252	0.0170 -0.3253	0.0394 -0.3265	0.0616 -0.3283
0.45 0.157 -0.1344	0.0222 -0.1349	0.0490 -0.1366	0.0758 -0.1392
0.50 0.129 0.0222	0.0291 0.0264	0.0614 0.0239	0.0936 0.0262
0.55 0.0192 0.1877	0.0387 0.1965	0.0779 0.1828	0.1774 0.1168
0.60 0.0293 0.3546	0.0525 0.3526	0.1005 0.3468	0.1479 0.3386
0.65 0.0429 0.5362	0.0731 0.5329	0.1329 0.5236	0.1914 0.5163
0.70 0.0646 0.7437	0.1054 0.7381	0.1814 0.7226	0.2550 0.7019
0.75 0.1070 0.941	0.1585 0.9336	0.2581 0.9566	0.3526 0.9212
0.80 0.1412 1.312	0.2157 1.2527	0.3879 1.2440	0.5113 1.1796
0.85 0.5315 1.7603	0.4367 1.7162	0.6265 1.6395	0.7866 1.4922
0.90 0.6446 2.4263	0.8473 2.3137	1.1092 2.0598	1.2922 1.7947
0.95 1.7124 3.4487	1.9283 3.0949	2.1525 2.4405	2.2126 1.9014
1.00 5.1312 3.7410	4.7106 2.8443	3.9455 1.7582	3.3597 1.1603
1.05 0.3542 -1.9606	0.4858 -1.3368	0.2674 -0.7195	0.4577 -0.4546
1.10 2.6497 -2.9449	2.7570 -2.5378	2.6900 -1.8264	2.5089 -1.3393
1.15 1.3056 -2.2037	1.4322 -2.0315	1.5893 -1.6909	1.3829 -1.0490
1.20 0.7793 -1.5977	0.8759 -1.5196	1.0309 -1.5096	1.1363 -1.1811
1.25 0.5302 -1.1739	0.6054 -1.1327	0.7367 -1.0492	0.8419 -0.9415
1.30 0.3442 -0.6597	0.4565 -0.8356	0.5696 -0.7910	0.6677 -0.7213
1.35 0.3135 -0.6105	0.3676 -0.5956	0.4695 -0.5622	0.5619 -0.5257
1.40 0.2614 -0.4004	0.3122 -0.3912	0.4086 -0.3711	0.4981 -0.3566
1.45 0.2285 -0.2136	0.2778 -0.2083	0.3730 -0.1979	0.4527 -0.1883
1.50 0.2178 -0.0391	0.2584 -0.0370	0.3563 -0.0347	0.4489 -0.0333
1.55 0.1975 0.1315	0.2514 0.1305	0.3556 0.1246	0.4539 0.1136
1.60 0.1973 0.3259	0.2566 0.3212	0.3712 0.2855	0.4779 0.2622
1.65 0.2079 0.4921	0.2763 0.4924	0.4060 0.4533	0.5242 0.4156
1.70 0.2345 0.7002	0.3158 0.6826	0.4666 0.6333	0.5991 0.5697
1.75 0.2859 0.9443	0.3862 0.9131	0.5655 0.8302	0.7137 0.7299
1.80 0.3820 1.2453	0.5103 1.1983	0.7255 1.0461	0.8553 0.8971
1.85 0.5625 1.6361	0.7369 1.5247	0.9868 1.2714	1.0375 1.0198
1.90 0.9635 2.1591	1.1755 1.9215	1.4131 1.4590	1.4911 1.3752
1.95 1.8679 2.7495	2.0572 2.2496	2.0605 1.4539	2.9246 0.9568
2.00 0.0396 2.7033	3.5455 1.8339	2.7850 0.9691	2.3015 0.5732
2.05 5.4367 -0.3557	4.2701 -0.1374	3.0304 -0.0134	2.3989 0.0037
2.10 3.3406 -2.2772	3.0998 -1.5752	2.5661 -0.8202	2.1053 -0.4822
2.15 1.8152 -2.0877	1.9261 -1.6954	1.9127 -1.0959	1.7833 -0.7240
2.20 1.1143 -1.6269	1.2508 -1.4267	1.4092 -1.0537	1.4391 -0.7647
2.25 0.7683 -1.2369	0.8977 -1.1272	1.0770 -0.8998	1.1776 -0.6975
2.30 0.5773 -0.9277	0.6081 -0.8629	0.8640 -0.7211	0.9841 -0.5843
2.35 0.4626 -0.6754	0.5603 -0.6353	0.7270 -0.5454	0.8555 -0.4551
2.40 0.3936 -0.4603	0.4799 -0.4352	0.6394 -0.3792	0.7710 -0.3226
2.45 0.3442 -0.2685	0.4296 -0.2534	0.5858 -0.2217	0.7196 -0.1915
2.50 0.3156 -0.0895	0.4006 -0.0824	0.5578 -0.0705	0.6947 -0.0627

Normalized Admittance Y/Δ of Loop Antennas in Dissipative Media

$\Omega = 20$										
$\frac{\alpha}{\beta}$	$\frac{\alpha}{\beta} = 0.10$			$\frac{\alpha}{\beta} = 0.30$			$\frac{\alpha}{\beta} = 0.50$			$\frac{\alpha}{\beta} = 1.00$
	Y/Δ	$\frac{Y}{\Delta}$	$\frac{Y}{\Delta}$	Y/Δ	$\frac{Y}{\Delta}$	$\frac{Y}{\Delta}$	Y/Δ	$\frac{Y}{\Delta}$	$\frac{Y}{\Delta}$	
0.05	0.0113	-6.3815	0.0338	-6.3861	0.0562	-6.3952	0.0786	-6.4087	0.1120	-6.4375
0.10	0.0229	-3.1070	0.0682	-3.1164	0.1132	-3.1351	0.1578	-3.1629	0.2237	-3.2217
0.15	0.0351	-1.9772	0.1038	-1.9920	0.1717	-2.0214	0.2383	-2.0648	0.3349	-2.1557
0.20	0.0480	-1.3823	0.1414	-1.4036	0.2326	-1.4452	0.3207	-1.5062	0.4448	-1.6322
0.25	0.0622	-0.9999	0.1816	-1.0290	0.2966	-1.0852	0.4051	-1.1666	0.5524	-1.3310
0.30	0.0780	-0.7220	0.2254	-0.7611	0.3645	-0.8349	0.4917	-0.9399	0.6560	-1.1458
0.35	0.0959	-0.5020	0.2738	-0.5538	0.4369	-0.6495	0.5800	-0.7817	0.7533	-1.0313
0.40	0.1169	-0.3157	0.3281	-0.3845	0.5143	-0.5072	0.6690	-0.6706	0.8421	-0.9639
0.45	0.1420	-0.1495	0.3897	-0.2410	0.5968	-0.3972	0.7571	-0.5950	0.9202	-0.9296
0.50	0.1728	0.0053	0.4606	-0.1169	0.6842	-0.3141	0.8421	-0.5481	0.9859	-0.9182
0.55	0.2117	0.1567	0.5425	-0.0993	0.7750	-0.2552	0.9211	-0.5250	1.0386	-0.9221
0.60	0.2624	0.3084	0.6375	0.0820	0.8669	-0.2197	0.9914	-0.5214	1.0788	-0.9351
0.65	0.3305	0.4651	0.7467	0.1545	0.9563	-0.2069	1.0504	-0.5326	1.1079	-0.9523
0.70	0.4251	0.6303	0.8698	0.2031	1.0384	-0.2155	1.0967	-0.5540	1.1279	-0.9706
0.75	0.5609	0.8048	1.0034	0.2209	1.1084	-0.2423	1.1300	-0.5807	1.1409	-0.9877
0.80	0.7619	0.9825	1.1388	0.2009	1.1621	-0.2824	1.1516	-0.6086	1.1492	-1.0027
0.85	1.0632	1.1375	1.2616	0.1399	1.1974	-0.3293	1.1635	-0.6345	1.1544	-1.0153
0.90	1.5000	1.1974	1.3544	0.0430	1.2149	-0.3765	1.1683	-0.6566	1.1578	-1.0256
0.95	2.0413	1.0150	1.4031	-0.0744	1.2174	-0.4185	1.1686	-0.6739	1.1604	-1.0340
1.00	2.4573	0.4673	1.4043	-0.1905	1.2096	-0.4518	1.1667	-0.6868	1.1626	-1.0410
1.05	2.4343	-0.2422	1.3669	-0.2858	1.1958	-0.4752	1.1641	-0.6956	1.1648	-1.0470
1.10	2.0421	-0.7142	1.3069	-0.3501	1.1803	-0.4893	1.1619	-0.7015	1.1670	-1.0523
1.15	1.5945	-0.8641	1.2401	-0.3927	1.1658	-0.4956	1.1606	-0.7052	1.1693	-1.0573
1.20	1.2458	-0.8260	1.1779	-0.3889	1.1542	-0.4963	1.1605	-0.7076	1.1716	-1.0620
1.25	1.0062	-0.7116	1.1267	-0.3761	1.1463	-0.4932	1.1616	-0.7093	1.1738	-1.0667
1.30	0.8488	-0.5744	1.0889	-0.3513	1.1422	-0.4882	1.1636	-0.7109	1.1759	-1.0712
1.35	0.7483	-0.4351	1.0648	-0.3201	1.1416	-0.4826	1.1663	-0.7127	1.1779	-1.0758
1.40	0.6881	-0.3003	1.0532	-0.2868	1.1439	-0.4775	1.1695	-0.7148	1.1797	-1.0803
1.45	0.6577	-0.1716	1.0526	-0.2546	1.1485	-0.4736	1.1729	-0.7174	1.1813	-1.0847
1.50	0.6514	-0.0487	1.0613	-0.2258	1.1545	-0.4712	1.1762	-0.7203	1.1827	-1.0891
1.55	0.6666	0.0690	1.0771	-0.2022	1.1613	-0.4706	1.1795	-0.7236	1.1839	-1.0935
1.60	0.7030	0.1815	1.0981	-0.1848	1.1683	-0.4715	1.1825	-0.7272	1.1849	-1.0977
1.65	0.7619	0.2876	1.1222	-0.1744	1.1749	-0.4738	1.1852	-0.7309	1.1857	-1.1019
1.70	0.8458	0.3841	1.1472	-0.1710	1.1810	-0.4772	1.1876	-0.7347	1.1863	-1.1060
1.75	0.9578	0.4645	1.1711	-0.1742	1.1863	-0.4814	1.1897	-0.7386	1.1868	-1.1100
1.80	1.0993	0.5178	1.1921	-0.1831	1.1906	-0.4361	1.1916	-0.7424	1.1931	-1.1139
1.85	1.2660	0.5280	1.2090	-0.1963	1.1941	-0.4909	1.1932	-0.7462	1.1973	-1.1177
1.90	1.4425	0.4769	1.2210	-0.2120	1.1969	-0.4956	1.1946	-0.7499	1.1973	-1.1215
1.95	1.5982	0.3543	1.2279	-0.2284	1.1990	-0.5002	1.1959	-0.7535	1.1973	-1.1252
2.00	1.6933	0.1719	1.2301	-0.2411	1.2006	-0.5044	1.1970	-0.7571	1.1971	-1.1288
2.05	1.7011	-0.0310	1.2286	-0.2577	1.2020	-0.5083	1.1981	-0.7605	1.1863	-1.1324
2.10	1.6264	-0.2059	1.2244	-0.2686	1.2031	-0.5118	1.1990	-0.7639	1.1864	-1.1359
2.15	1.5014	-0.3217	1.2188	-0.2762	1.2042	-0.5150	1.1998	-0.7672	1.1859	-1.1392
2.20	1.3621	-0.3741	1.2128	-0.2808	1.2053	-0.5180	1.2006	-0.7705	1.1853	-1.1426
2.25	1.2334	-0.3749	1.2074	-0.2827	1.2064	-0.5208	1.2013	-0.7738	1.1846	-1.1459
2.30	1.1271	-0.3404	1.2033	-0.2925	1.2076	-0.5235	1.2019	-0.7770	1.1838	-1.1491
2.35	1.0463	-0.2841	1.2007	-0.2809	1.2089	-0.5261	1.2025	-0.7802	1.1829	-1.1523
2.40	0.9922	-0.2157	1.1999	-0.2784	1.2102	-0.5287	1.2029	-0.7834	1.1820	-1.1554
2.45	0.9565	-0.1415	1.2008	-0.2758	1.2116	-0.5314	1.2033	-0.7865	1.1809	-1.1585
2.50	0.9433	-0.0659	1.2033	-0.2736	1.2129	-0.5341	1.2037	-0.7897	1.1798	-1.1615

## BASIC T R. DISTRIBUTIONS LIST\*

Defense Documentation Center [40] DDA Cameron Station Alexandria, Virginia 22104	Mr. AECBL (CRXL) [6] L. G. Hanscom Field Bedford, Mass. 01731 [1] CRXL [1] CRD [1] CRW	Bendix Corporation Org. 1411, Bendix Base Albuquerque, New Mexico Attn: Dr. C. W. Harrison, Jr.	Professor Jerome N. Singer Div. of Electrical Engineering University of California Berkeley 4, California
Activity Supply Office [10] Building 1004 Charles Wood Annex East Monmouth, New Jersey Attn: Director of Research	Commanding General [1] Air Research and Development Command P.O. Box 1595 Baltimore 3, Maryland Attn: KDTARP	Bendix Corporation Bendix Base Albuquerque, New Mexico Attn: Library Division 1922-1	Professor Charles Kittel Department of Physics University of California Berkeley 4, California
Commanding Officer [10] Office of Naval Research Navy 100, Box 19 Fleet Post Office New York, New York	Director, Air University [2] Library Maxwell Air Force Base Alabama	National Bureau of Standards Library Room 101, Northwest Bldg Washington 25, D.C.	Dr. C. H. Papas Dept. of Electrical Engineering California Institute of Technology Pasadena, California
Chief of Naval Research [4] Department of the Navy Washington 25, D.C. Attn: Code 427, Dr. Shantz	Commanding General [2] Air Force Development Center Griffiss Air Force Base Rome, New York	Librarian U. S. Department of Commerce National Bureau of Standards Boulder, Colorado	Professor H. G. Booker School of Electrical Engineering Cornell University Ithaca, New York
Commanding Officer [3] Office of Naval Research 495 Summer Street Boston, Massachusetts	Commanding General Rome Air Development Center Griffiss Air Force Base Rome, New York Attn: RCREC-4C	U. S. Coast Guard 1300 E. Street, N.W. Washington 25, D.C. Attn: EEE	Dr. C. J. Falbeneck Bassett Memorial Institute Columbus, Ohio Attn: Electrical Engineering Div
Chief of Naval Research Department of the Navy Washington 25, D.C. Attn: Code 421	Commanding General Rome Air Development Center Griffiss Air Force Base Rome, New York Attn: RCR	Standard Electronics Lab. Stanford University Stanford, California Attn: Document Library Appl. 1 Electronics Lab.	Professor A. W. Stratton Dept. of Electrical Engineering University of Texas Austin 12, Texas
Commanding Officer Office of Naval Research John Cramer Library Building 80 East Randolph Street Chicago 1, Illinois	Air Force Office of Scientific Research Air Research and Development Command Washington 25, D.C. Attn: SKY, Physics Division	Library, Room A 229 Lincoln Laboratory P. O. Box 73 Lexington 73, Massachusetts	Charles C. H. Tang Bell Telephone Lab. Murray Hill, New Jersey
Commanding Officer Office of Naval Research 44 Broadway New York 13, New York	Commandant Air Force Institute of Technology Wright-Patterson Air Force Base Ohio Attn: Library	Mr. John Hewitt Document Room Research Lab. of Electronics Mass. Institute of Technology Cambridge 39, Massachusetts	Space Sciences Lab. Lawrence Observatory University of California Berkeley 4, California Attn: Dr. Samuel Silver
Commanding Officer Office of Naval Research 1010 East Green Street Pasadena, California	AF Research Division [2] Aeronautical Research Lab. (ARL) Wright-Patterson AF Base Ohio	Professor A. Van Hippel Mass. Institute of Technology Lab. for Insulation Research Cambridge 39, Massachusetts	Prof. A. W. Lawson Department of Physics University of California Riverside California
Commanding Officer Office of Naval Research 1000 Geary Street San Francisco 4, California	6570 AMRL (Library) Wright-Patterson Air Force Base Ohio	Library, College of Engineering University Heights Library University Heights New York University New York 33, New York	Professor Joseph E. Rowe Electron Physics Lab. Dept. of Electrical Engineering University of Michigan 1505 East Engineering Bldg. Ann Arbor, Michigan
The Director [4] Naval Research Laboratory Washington 25, D.C. Attn: Technical Information Officer	ARL/ARL/Mr. R. E. Woodward Building 450 Wright-Patterson AF Base Ohio	E. A. Chapman, Librarian Rensselaer Polytechnic Institute Ames Eaton Hall Troy, New York	Gordon McKay Library [2] Pierce Hall, Harvard University Oxford St., Cambridge, Mass.
Head, Document Section Technical Information Division Naval Research Laboratory Washington 25, D.C.	AF Special Weapons Center Kirtland Air Force Base Albuquerque, New Mexico Attn: SWO1	Dept. of Electrical Engineering Case Institute of Technology University Circle Cleveland 6, Ohio Attn: S. Seely, Head	Chung Kung University Electrical Engineering Department Taiwan, Taiwan Republic of China Attn: Prof. Chao-Hsi-Chou Head, Engineering Dept.
Martin A. Gorstens Magneton Branch, Code 6450 Solid State Division Naval Research Laboratory Washington 25, D.C.	Headquarters AF Missile Test Center MU-135, ADRC Patrick Air Force Base Florida	Robert Plonsey Department of Engineering Case Institute of Technology University Circle Cleveland 6, Ohio	Mr. D. J. Jones Department of Mathematics Univ. College of No. Staffordshire Keele Staffordshire, England
Assistant Secretary of Defense (Research and Development) Research and Development Board Department of Defense Washington 25, D.C.	Chief, European Office ARDC Command Shell Building 60 Rue Rayenstein Brussels, Belgium	Librarian Engineering Library Brown University Providence, Rhode Island	Professor Paul Sanai Mito Osaka City University Dept. of Engineering Sciences 12 Nishi Ogimachi Kitaku Osaka, Japan
Chief of Naval Operations Department of the Navy Washington 25, D.C. Attn: Op-20	Headquarters Air Research and Development Command United States Air Force Andrews Air Force Base Washington 25, D.C.	Secretary, Working Group Semiconductor Devices 346 Broadway, 8th Floor New York 13, New York Attn: AGET	Contract Nonr-1866 (28) only Dept. of Electrical Engineering King's College Newcastle upon Tyne England
Chief of Naval Operations Department of the Navy Washington 25, D.C. Attn: Op-43	Mr. A. D. Bedrosian Signals Corps Liaison Office Mass. Institute of Technology Building 26, Room 131 Cambridge 31, Massachusetts	Institute for Defense Analysis Communications Research Div. von Neumann Hall Princeton	Contract Nonr-1866 (12) only U. S. Atomic Energy Commission Office of Technical Information Extension P. O. Box 62 Oak Ridge Tennessee
Chief, Bureau of Ships [2] Department of the Navy Washington 25, D.C. Attn: Code 410	Dr. J. Anton Hoffman Ordnance Materials Res. Office Watertown Arsenal Watertown, Massachusetts	Ohio State University Research Foundation 1314 Kinnear Road Columbus 12, Ohio Attn: Reports Library	----- *One copy to each address unless otherwise specified by numbers in brackets
Commander [2] U. S. Naval Electronics Lab San Diego, California	Commanding Officer [3] U. S. Army Research Office Attn: CRXA/AR Mr. Ush Box CM, Duke Station Durham, North Carolina	Polytechnic Institute of Brooklyn Graduate Center Route 110 Farmington, New York	Ohio State University Research Foundation 1314 Kinnear Road Columbus 12, Ohio Attn: Antenna Library
Director Naval Ordnance Laboratory White Oak, Maryland	Commanding Officer U. S. Army Signal Missile Support Apt. 'Y' Attn: SIGWS-MEW Mr. T. S. Bellows White Sands Missile Range Mexico	Yale University Mason Laboratory 400 Temple Street New Haven 10, Conn. Attn: Library	University of New Mexico Dept. of Electrical Engineering Room 214 Albuquerque, New Mexico Attn: R. K. Moore, Chairman
Technical Library U. S. Naval Proving Ground Dahlgren, Virginia	U. S. Army Engineer Research and Development Laboratories Fort Belvoir, Virginia Attn: Technical Documents Center	Carlyle Berlin Laboratory [2] John Hopkins University Charles and 14th Street Baltimore 14, Maryland Attn: Librarian	Carlyle Berlin Laboratory [2] John Hopkins University Charles and 14th Street Baltimore 14, Maryland Attn: Librarian
Commanding Officer U. S. Air Development Center Johnsville, Pennsylvania Attn: NADC Library	National Security Agency [2] Physical Sciences Division Fort George Meade, Maryland Attn: Dr. Alvin Marbler	Associate Prof. A. Kaprielian Dept. of Electrical Engineering University of Southern California University Park Los Angeles 7, California	Donald C. Simpson Dept. of Electrical Engineering University of Arizona Tucson 25, Arizona
Commander U. S. Air Development Center Johnsville, Pennsylvania Attn: AAAC	Dr. H. Campbell National Security Agency Physical Sciences Division Fort George Meade, Maryland	Georgia Institute of Technology Georgia Tech Research Institute Atlanta 30332	
Librarian U. S. Naval Post Graduate School Monterey, California	Specialist Library Brandeis University Waltham, Massachusetts		
Mr. John F. Wallace Scientific and Technical Unit U.S. CIO/COMIAVAC Frankfurt, April 1971 U. S. Liaison Unit New York, NY			

**END**

**FILMED**

**9-85**

**DTIC**